

Unlocking the long tail of demand response: quantification and control

Simon Tindemans
s.tindemans@imperial.ac.uk

Contributions from Vincenzo Trovato, James Schofield, Miao Wei, Marko Aunedi and Goran Strbac



Four research themes

- Power systems and energy
- Power electronics
- Control theory and applications
- Smart grids [integration of other activities]

Maurice Hancock Smart Energy Lab

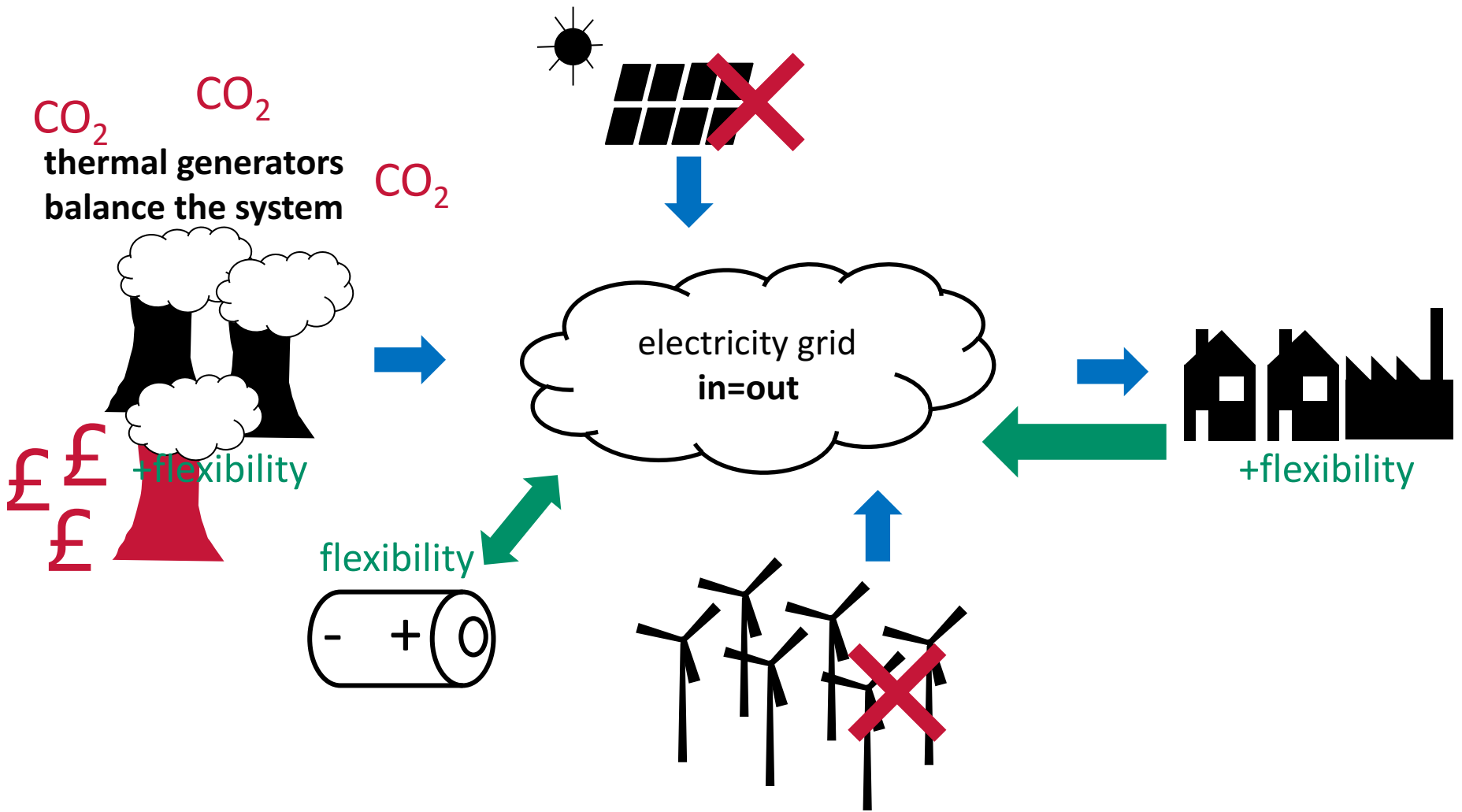
- Reconfigurable 8-node network
2x90kVA programmable voltage
supplies
- Rapid prototyping control system
(Simulink/Labview)



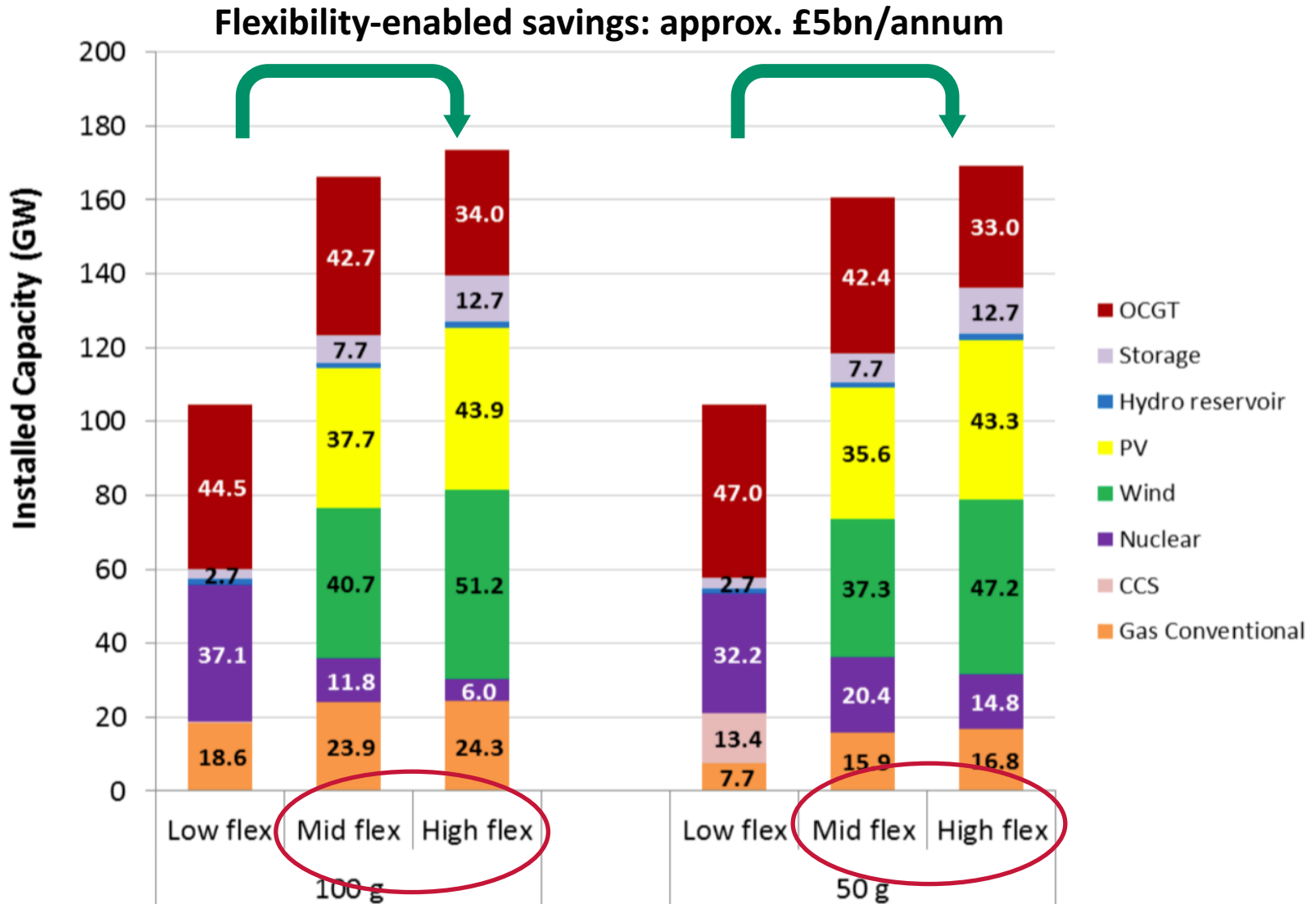
1. Introduction
2. Response to dynamic time-of-use tariffs
 - Peak shaving response
 - Household responsiveness
3. Controlling smart refrigerators
 - Stochastic controller
 - Aggregation
4. Final remarks

Business as usual approach limits the uptake of renewable generation

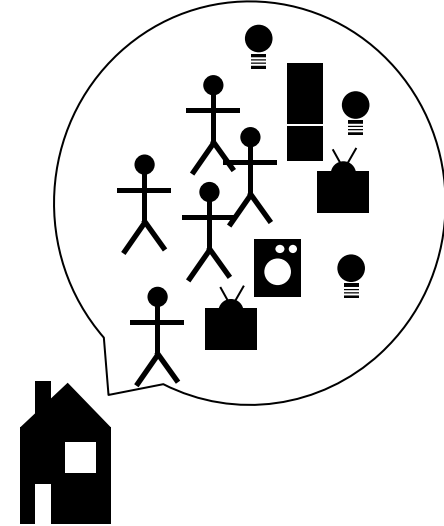
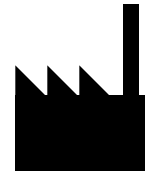
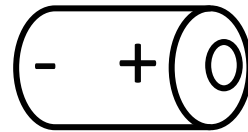
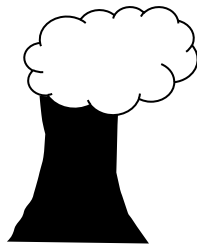
To achieve carbon emission and reliability targets in a cost-effective manner
we must *increase and exploit flexibility*



Flexibility and the optimal energy mix



The flexibility spectrum



source

Flexible
generators

Grid scale
storage

Industrial and
commercial DR

residential DR

**individual
magnitude**

10-100MW

1-1000MW

100kW - 1MW

10W – 1kW

number

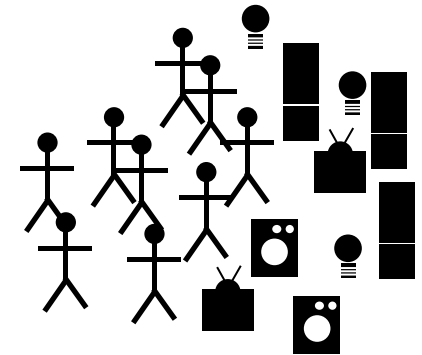
100

10 - 1000

1000 - 10000

10s of millions

**'Long tail' of
demand response**



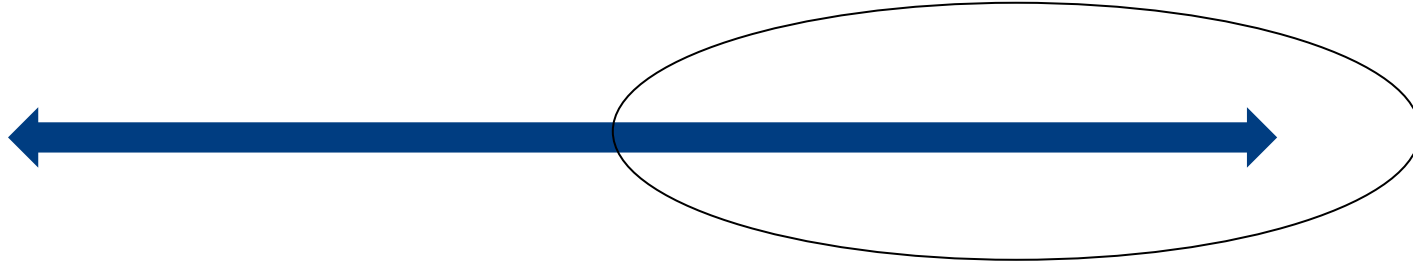
Constraints/challenges

- Flexibility is a by-product of other activities, which will affect service availability.
- Small per-device flexibility contribution, so cost *and* attention budget is small
- Significant heterogeneity

Opportunities

- Very large number of devices (at least at regional/national levels), so large-number statistics apply.
- Regular consumption patterns allow for aggregate prediction.

two examples



Direct control

Real time dispatch of resources

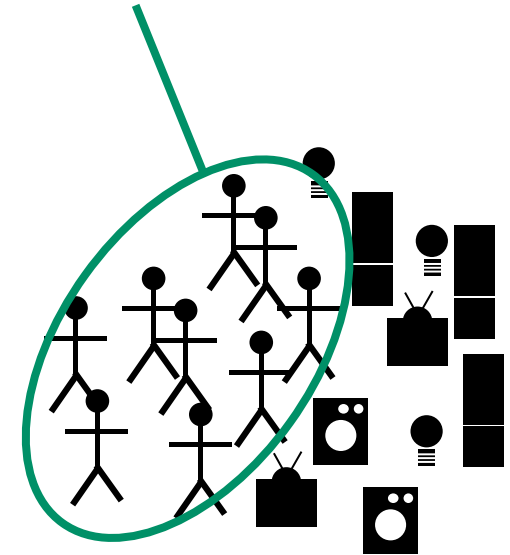
- ✓ • Accountability
- ✗ • Requires real-time communication
- ✗ • Limited autonomy
- ✗ • Privacy concerns

Indirect control

Decentralised response to non-local control signals (e.g. prices)

- ✓ • Autonomy
- ✓ • Low cost
- ? • Does it work?

User-mediated
demand response



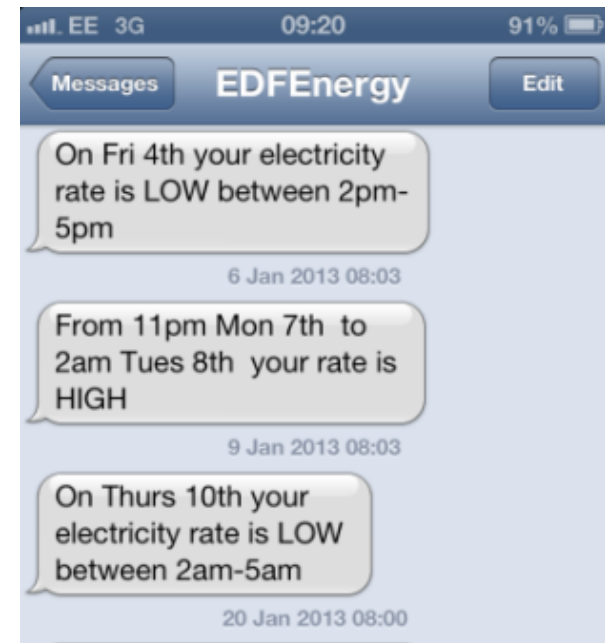
DYNAMIC TIME-OF-USE TARIFFS CHARACTERISING RESPONSIVENESS

The Low Carbon London demand response trials (2013)

5536 households with smart meters
(30-min kWh measurements)

1119 households took part in a **dynamic time of use trial**:

- Day ahead notification of prices via SMS and in-home displays
- Three price levels
 - Default: £0.1176/kWh
 - Low: £0.0399/kWh
 - High: £0.672/kWh

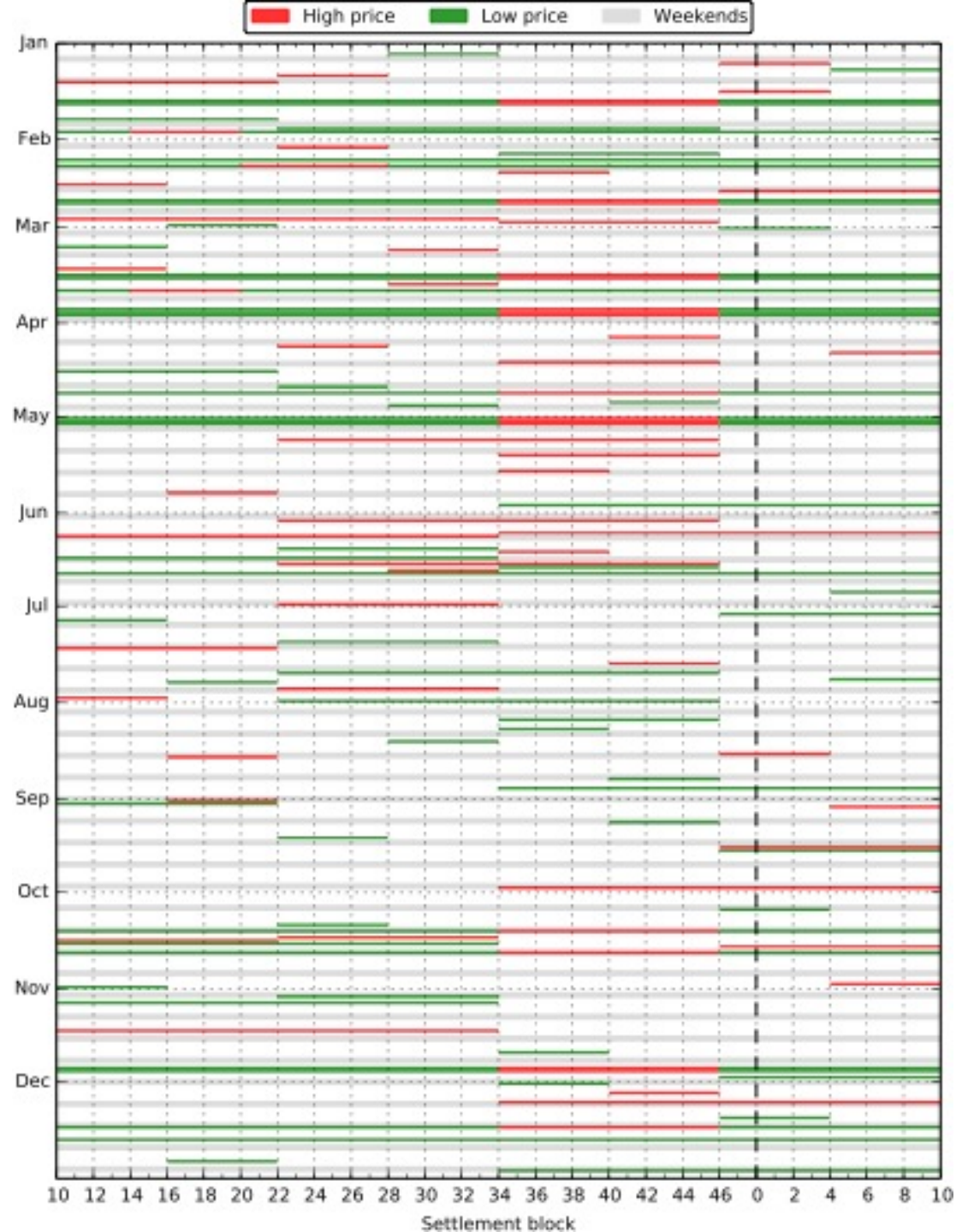


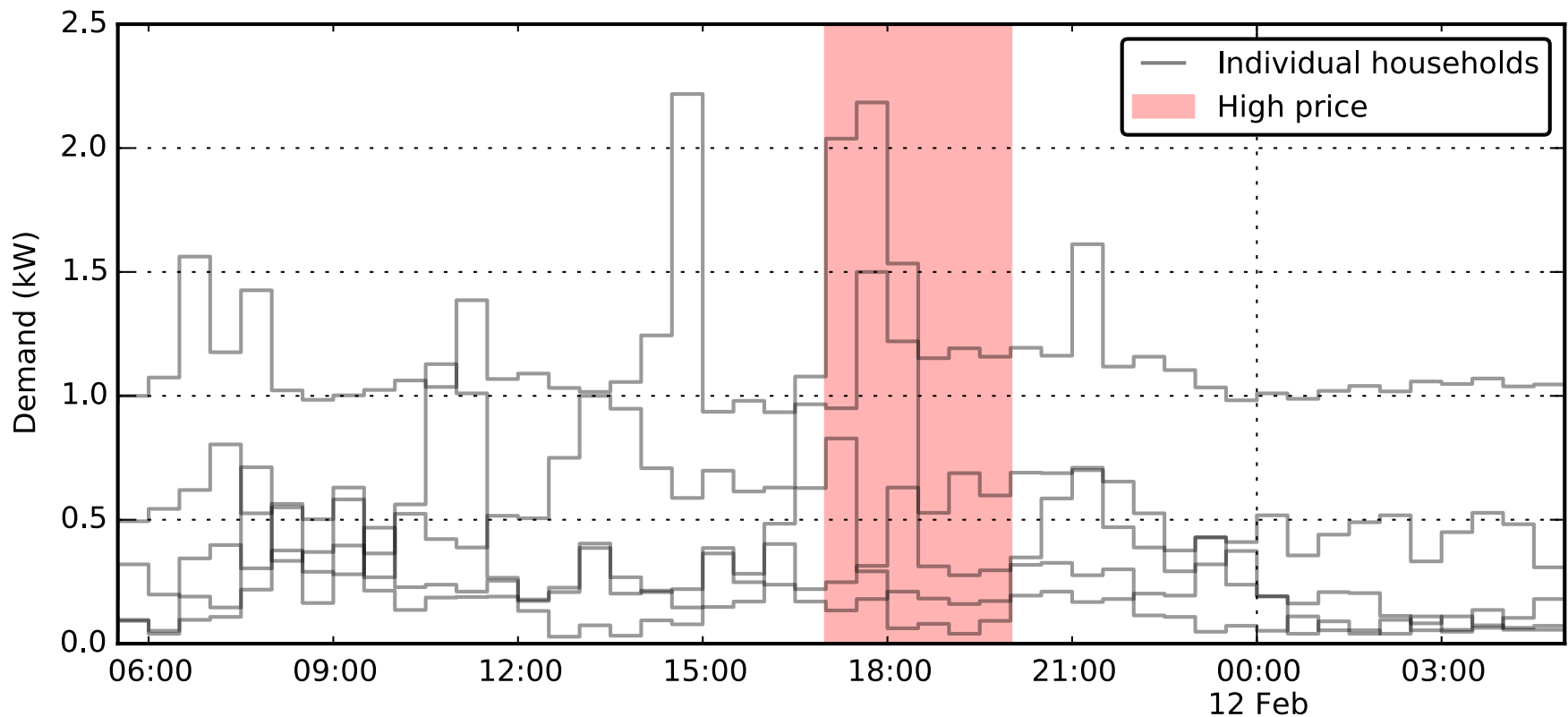
93 supply following events

- 45 high price events (3-12 hours)
- 48 low price events (3-24 hours)

13 constraint management events

- high price, flanked by low prices
- primarily targeted at evening peaks
- 1-3 consecutive days (21 days in total)





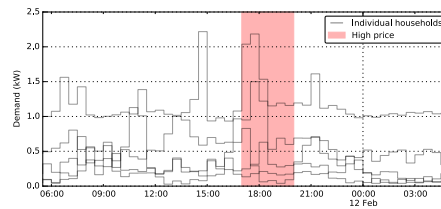
Dataset can be downloaded from UK Data Service

www.ukdataservice.ac.uk ; search for “Low Carbon London”

single event

many events

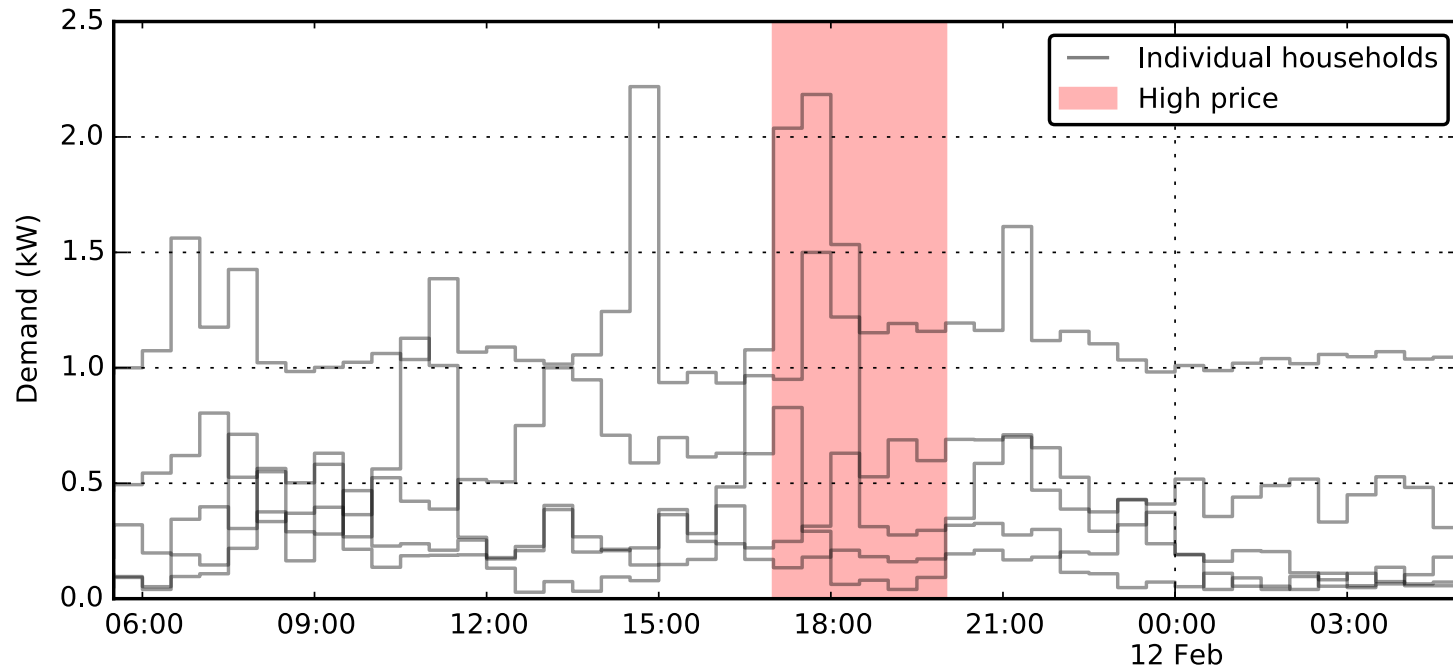
single
household



Topic 2:
Analysis of household
responsiveness

many
households

Topic 1:
Analysis of aggregate
response



Construct a linear regression model for the baseline, trained on non-event days.

$$B_t = \sum_{w=1}^W (\alpha_h d_{w,t} + \beta_w A^{\text{non-tou}}_t d_{w,t}) + \gamma m + \delta T_t$$

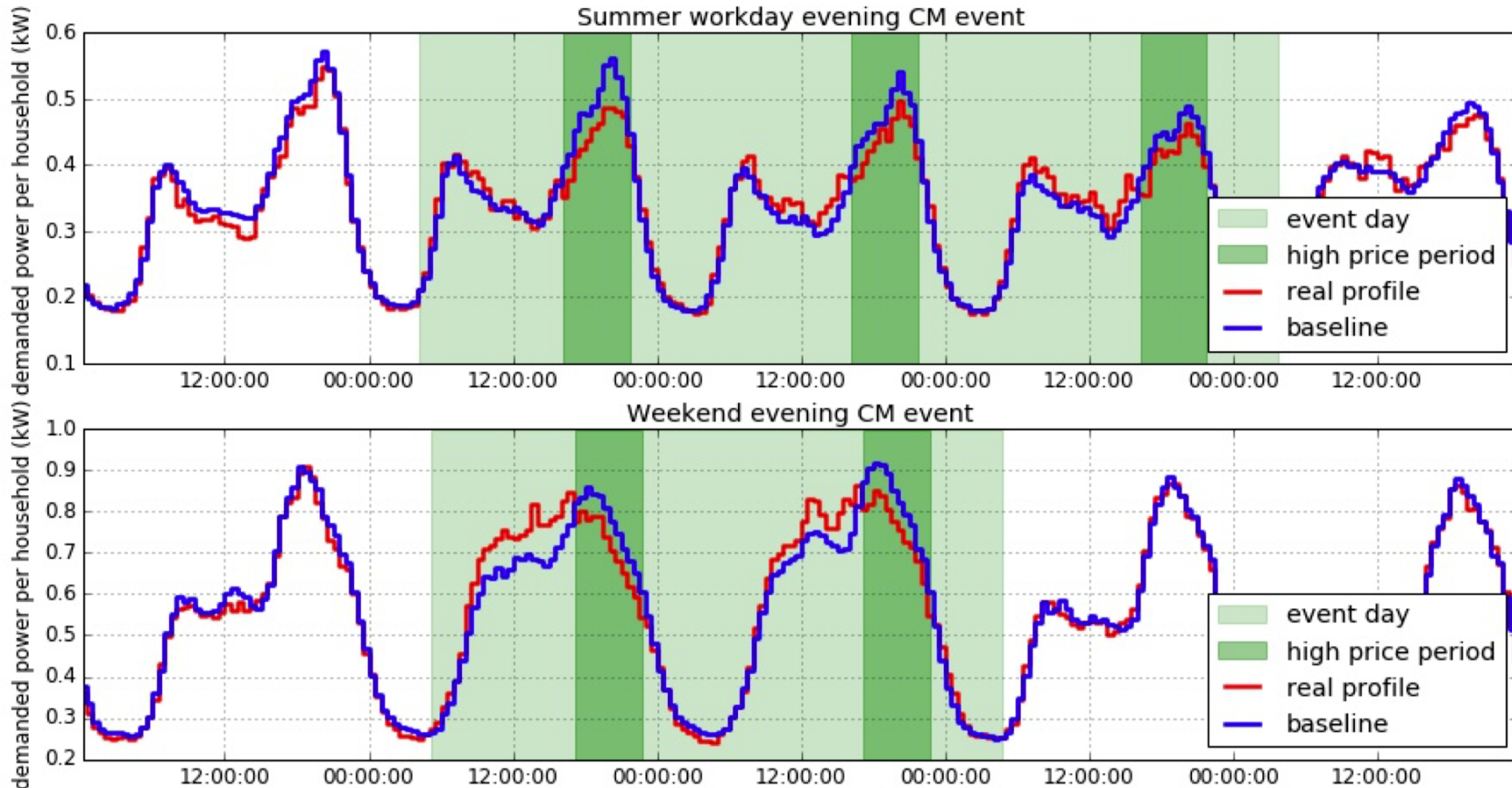
weekly profile

non-ToU group
consumption

trend line

temperature factor

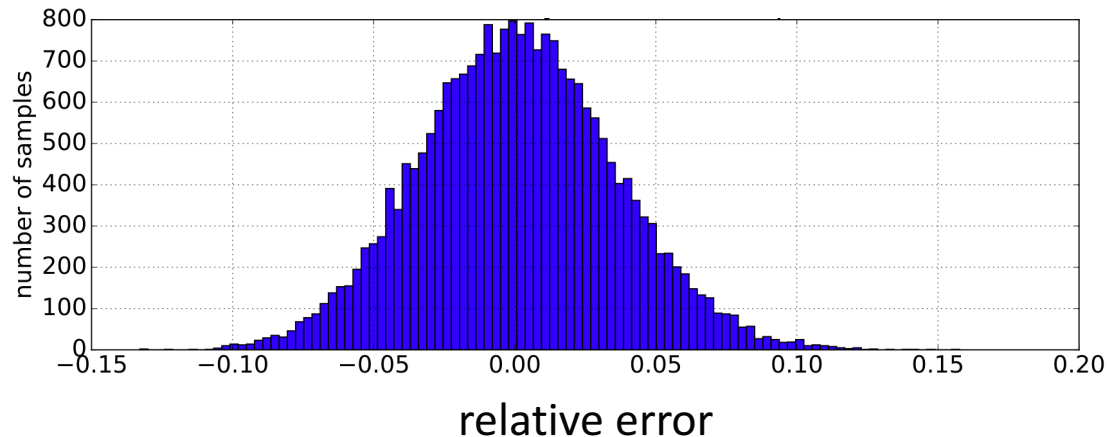
Example of measured response



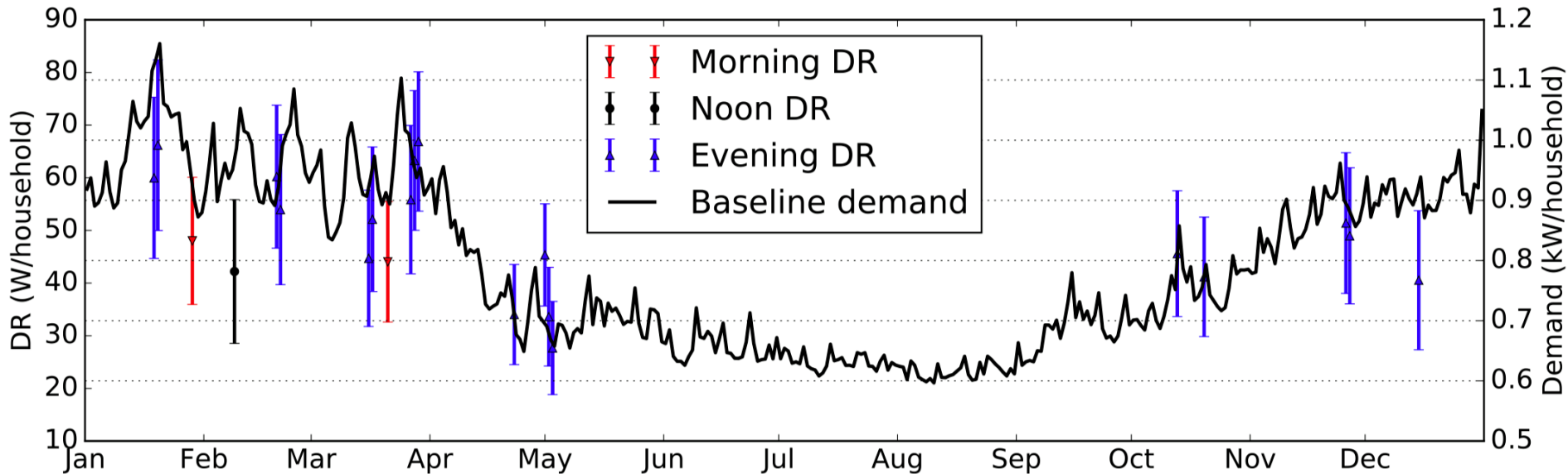
Bootstrap procedure

1. Resample the training data $N_{resample}$ times by selecting random days with replacement.
2. Train a baseline model for each resampled data set.
3. Compute the average out-of-bag error for each 30min settlement block.

Result: *Relative errors are normally distributed*



DR block	St Dev
30 mins	3.5%
3 hours	2.5%
6 hours	2.0%



Consider 21 *constraint management* events (peak shaving)

- High price at peak (evening, morning, weekend noon)
- Low price on either side of peak

Procedure

- Estimate DR using baseline model (averaged over block)
- Estimate error using baseline error model

1. Select simplest consistent model

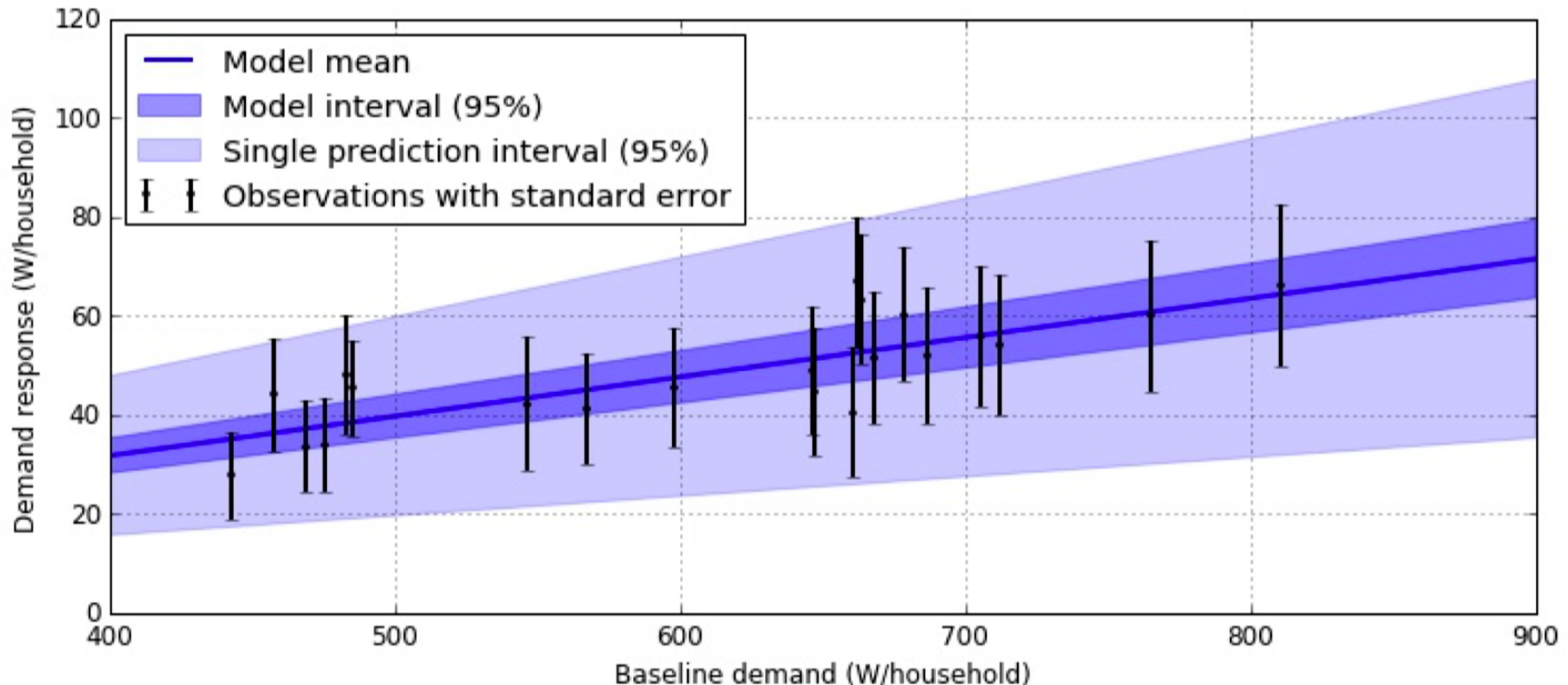
$$R_{CM}^{demand} = -0.079 \times [\text{baseline demand}] + (\text{random variation})$$

2. Model uncertainty = confidence of parameter fit

demand reduction between 7.1-8.8% of baseline demand (95% confidence)

3. Uncertainty of next measurement = model uncertainty + baseline variability

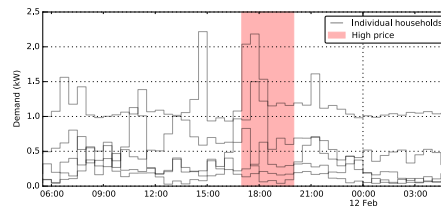
demand reduction between 4-12% of baseline demand (95% confidence)



single event

many events

single
household



Topic 2:
Analysis of household
responsiveness

many
households

Topic 1:
Analysis of aggregate
response

Naive approach: Change in bills

Compare actual bill with hypothetical bill on a flat tariff

- Only measures *success*, but not the intent
- Does not account for natural differences in consumption *magnitude*, *flexibility* and *pattern*

Proposed approach: resampling

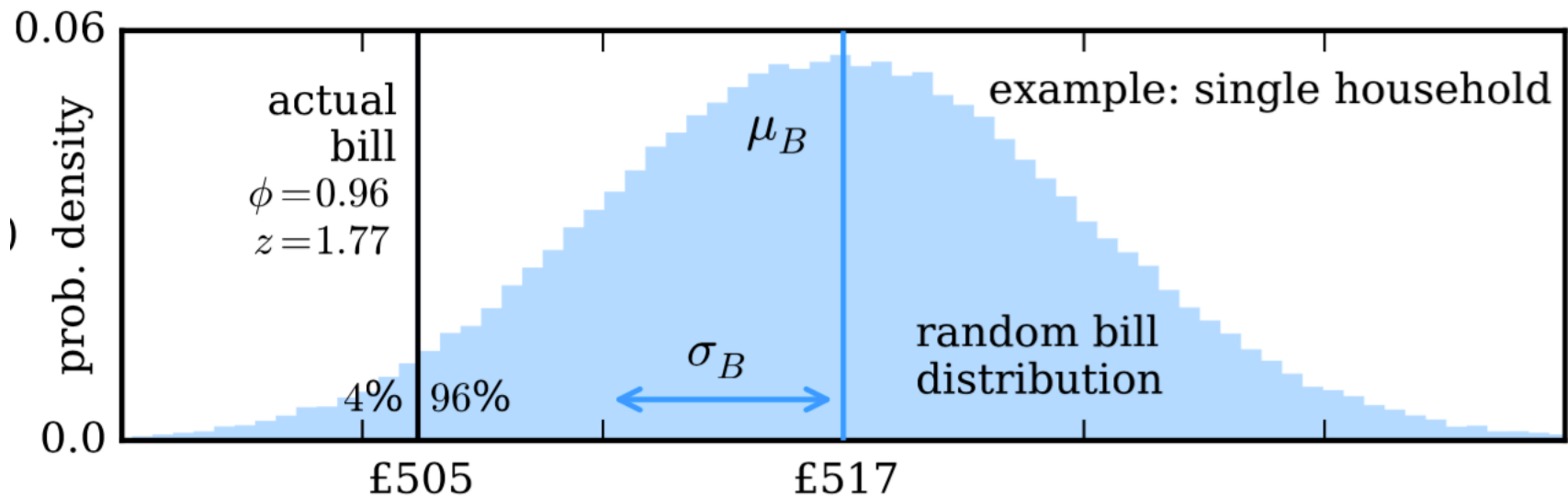
1. Compute the actual bill b^* using the actual price signal p_t and consumption c_t :

$$b^* = \sum_{t=1}^T p_t c_t$$

2. Generate randomised bills tariffs by permuting daily price signals

$$B = \sum_{t=1}^T p_{\Pi(t)} c_t$$

3. Compare the true and hypothetical bills

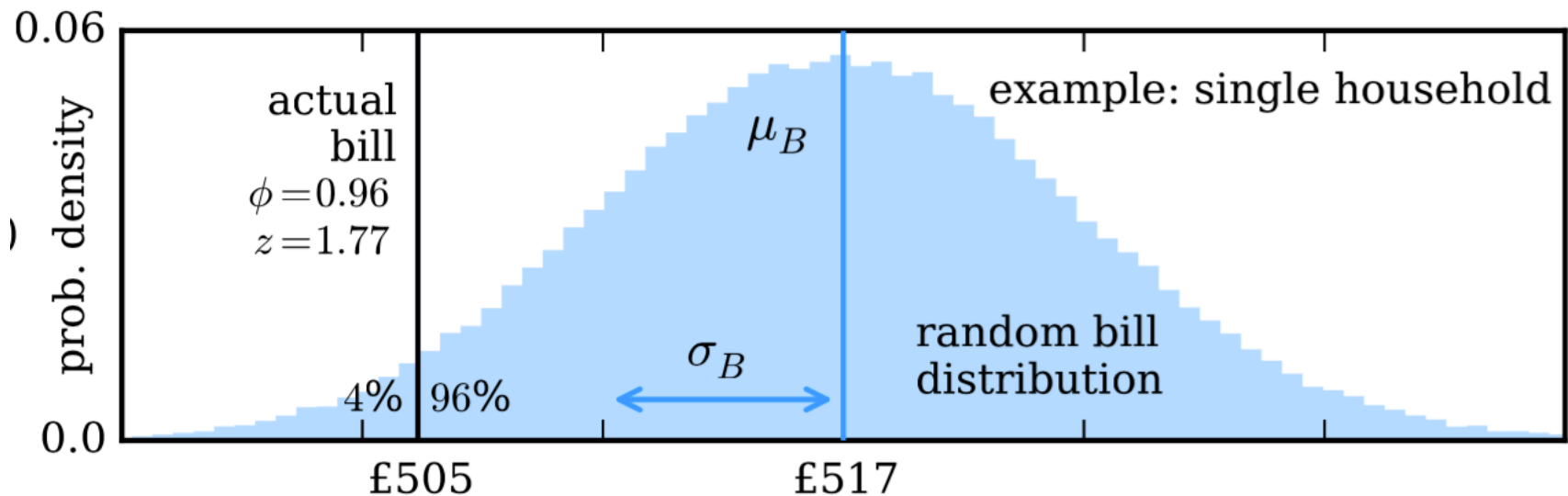


B is approximately normal [combinatorial CLT; Hoeffding, 1951].

Define a measure of responsiveness

$$\phi = \Pr(B > b^*) \quad \begin{array}{l} B \sim \text{random bill distribution} \\ b^* = \text{actual bill} \end{array}$$

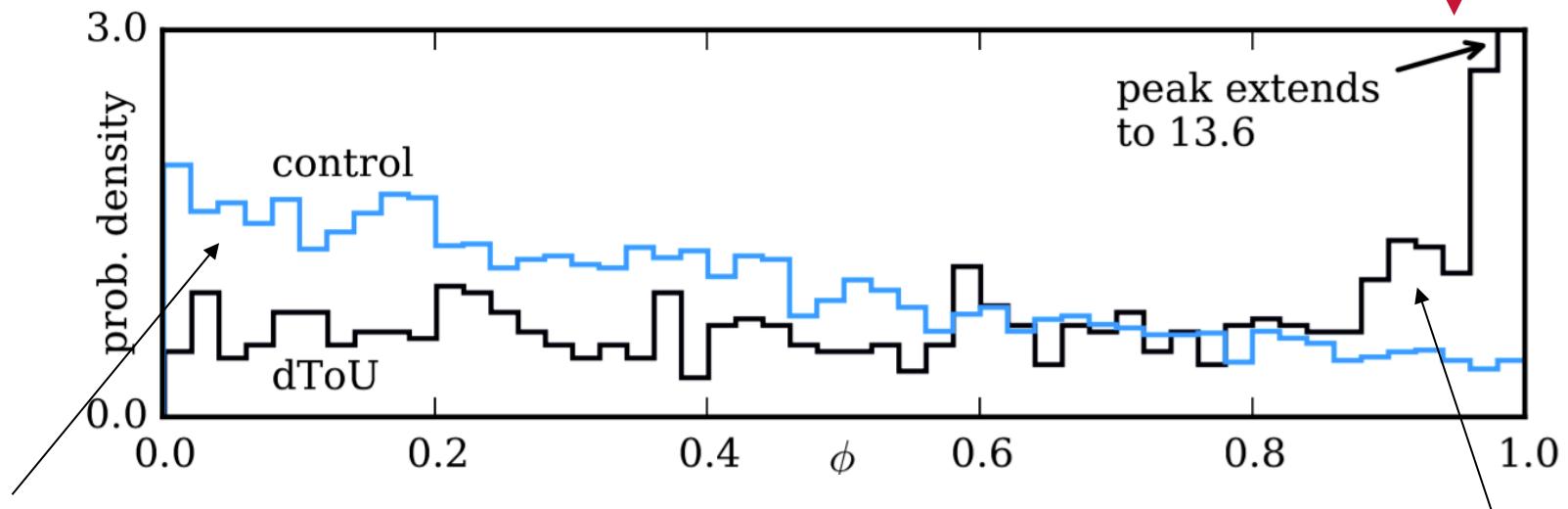
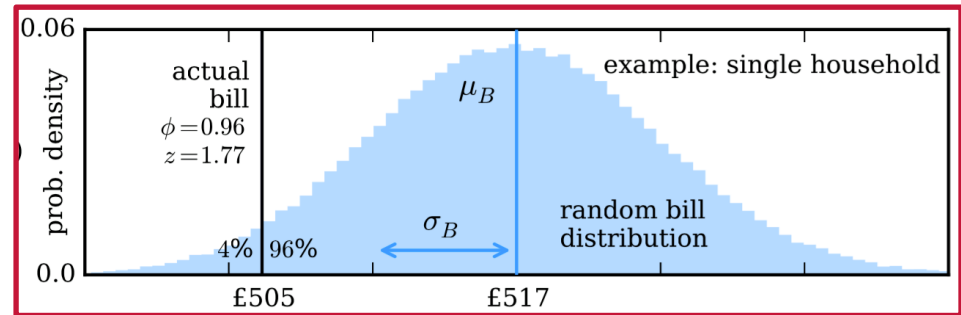
- Intuitive interpretation as a signal-to-noise measure.
- Provides a *confidence ranking* across households that correlates highly with stated actions (more so than DR measurements).



What makes a household 'responsive'?

1. Deliberate demand response
2. 'Accidental' demand response (both variable and constant) ← quantify
3. Price signal bias, relative to the population's consumption pattern (e.g. high prices that target winter peaks) ← eliminate

We can dig deeper using data from a control group

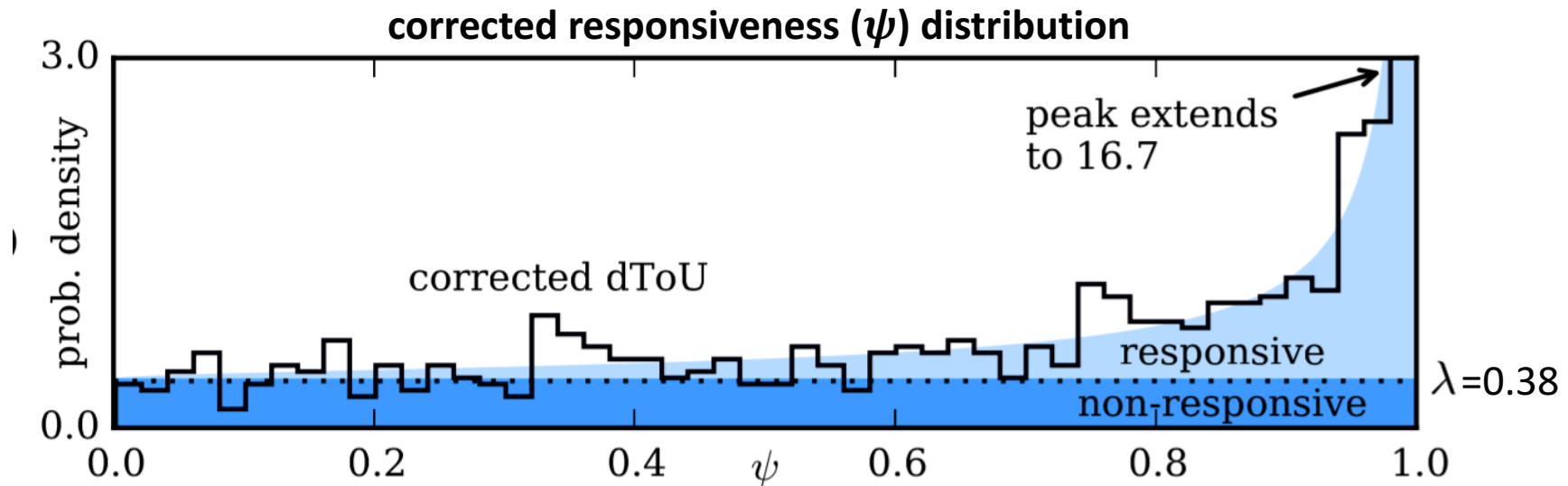


Evidence of price signal bias

Evidence of significant demand response

Use control group to create a new coordinate that corrects for price bias

$$\psi = F_{control}(\varphi)$$



Divide participants into **responsive** and **non-responsive sub-populations**

62% of households are responsive - but there is no need to state which is which.

Basis for a **probabilistic assessment of household responsiveness**:

$$\Pr(\text{responsive}|\psi) = \frac{f(\psi; \lambda) - \lambda}{f(\psi; \lambda)}$$

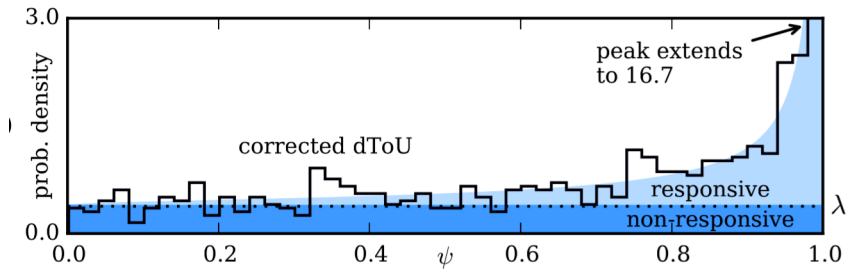


single event

many events

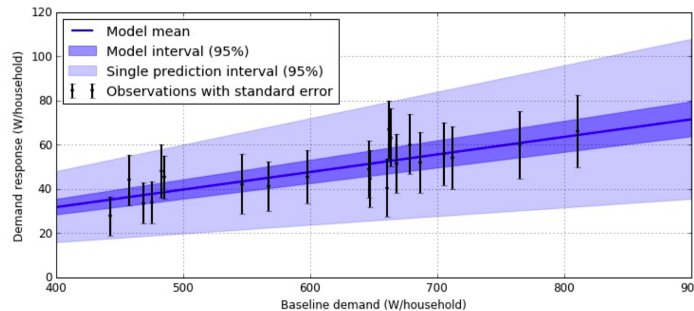
single household

online learning from
business as usual data



Nonparametric method to quantify
responsiveness
62% of participants were responsive

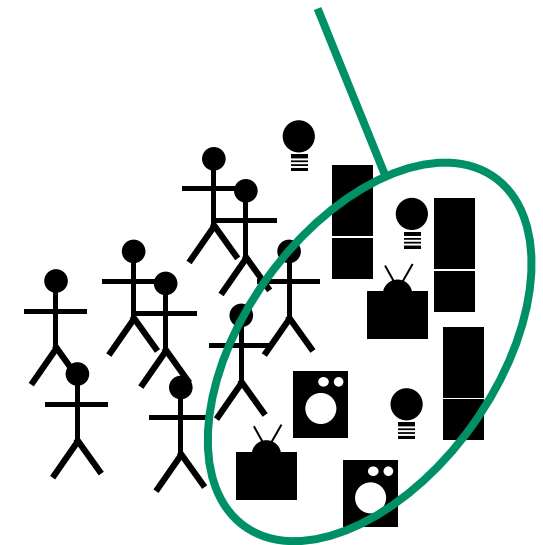
many households



Significant event-to-event variation in DSR peak shaving
4-12% reduction for the next event (95% confidence)



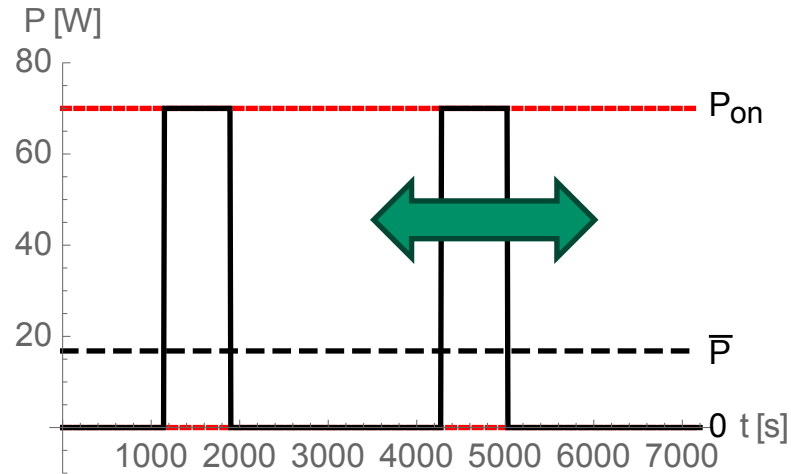
Automated
demand response



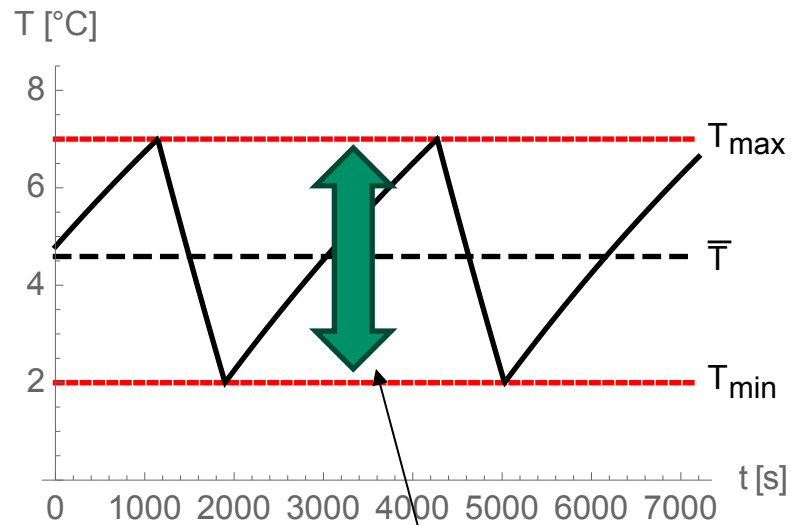
SMART REFRIGERATORS

DESIGNING A DECENTRALISED CONTROLLER

Power consumption



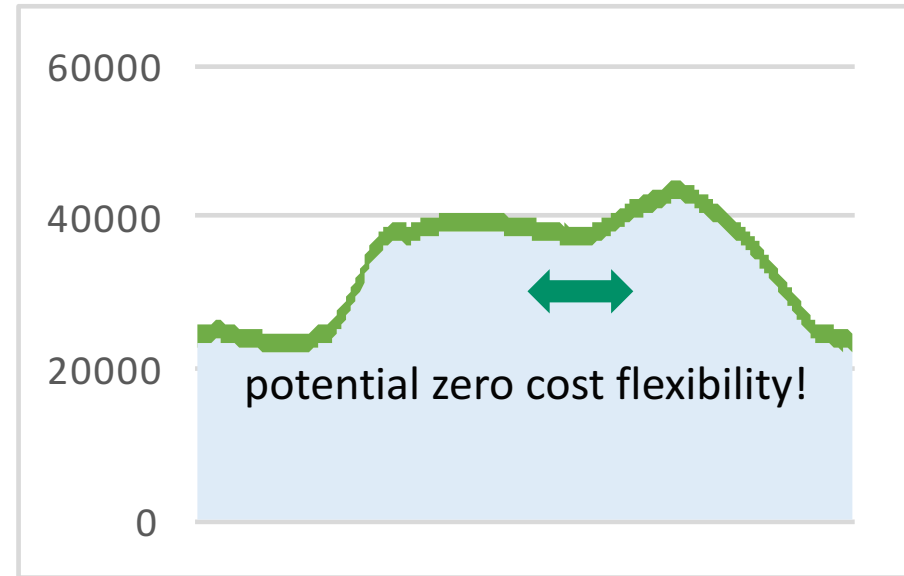
Temperature



source of flexibility

The opportunity

- Refrigerators represent 5-15% of system load (est. 2-3GW in GB)*
- Load shifting for ~30 minutes is free* **secondary use**



The challenge

- **Maintain cooling performance:** Secondary use (flexibility) should not compromise the primary use (cooling) of devices.
- **Robustness and scalability:** Reliance on real-time communication may result in bottlenecks and single points of failure
- **Controllability:** Ensure sufficient control over power consumption, and avoid *unwanted interactions*.

Our approach: semi-autonomous control

- *Collective goals* are set centrally
- *Actions* are decided locally, adapted to expected *group behaviour*

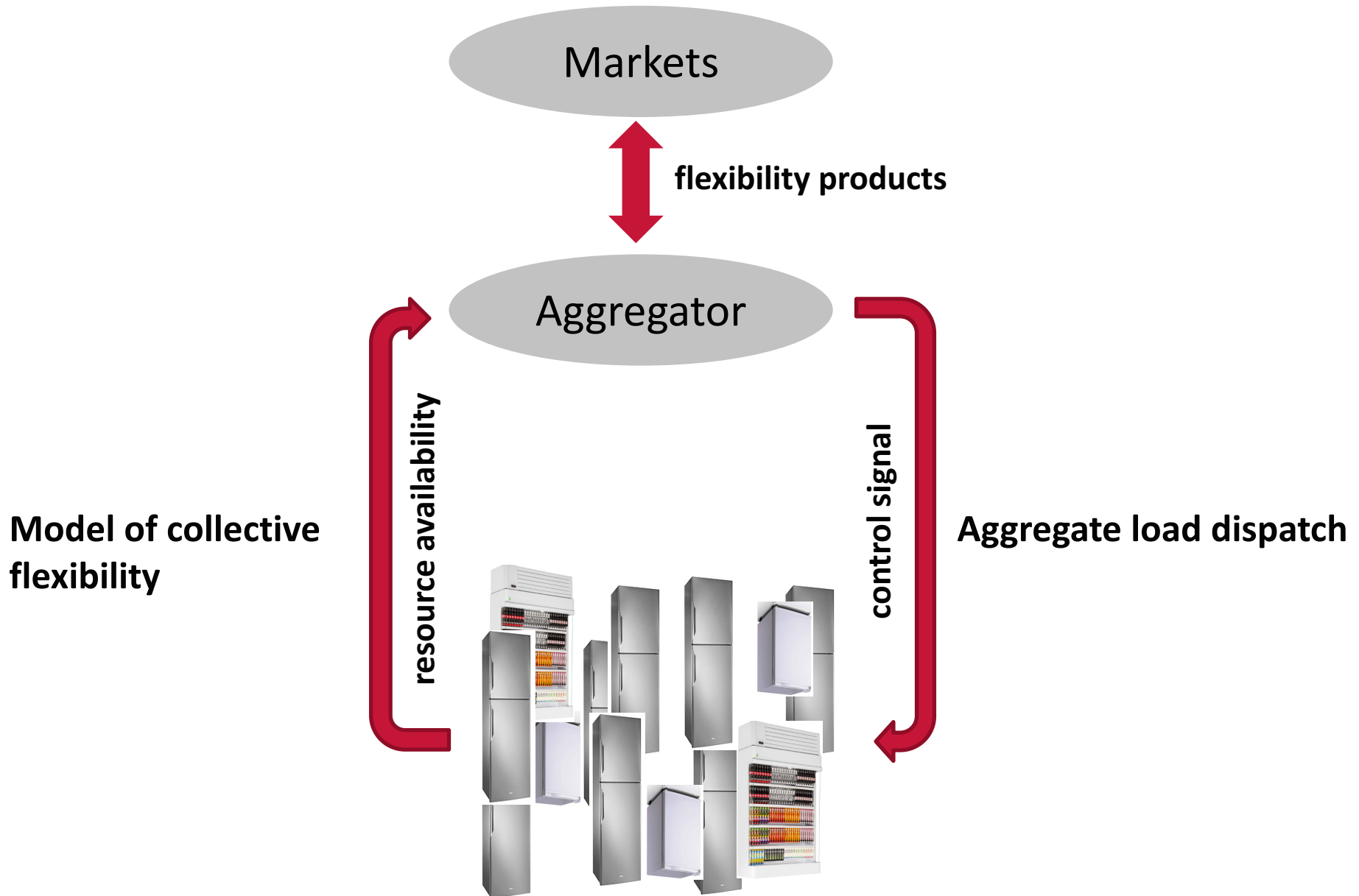


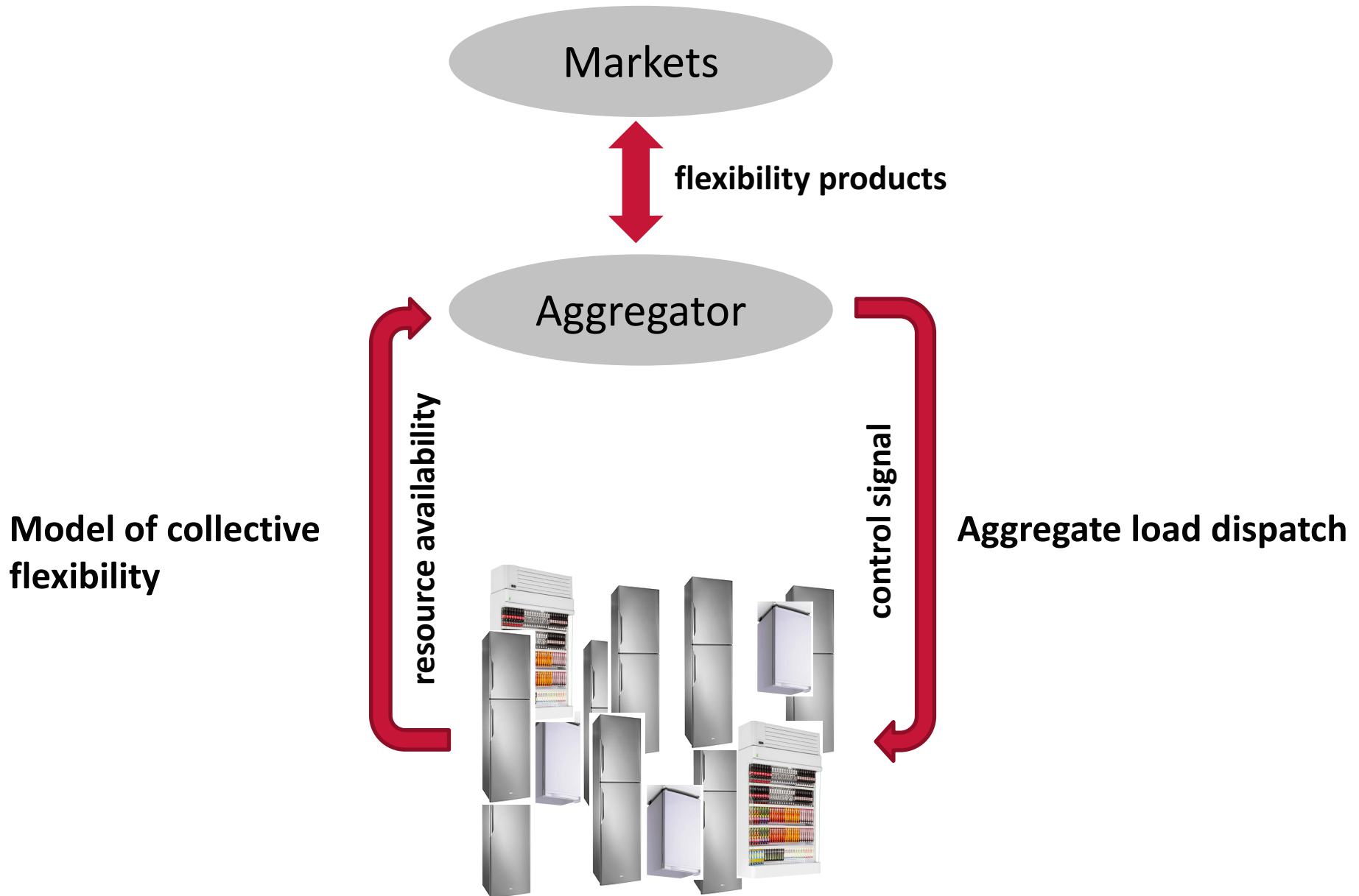
Direct control

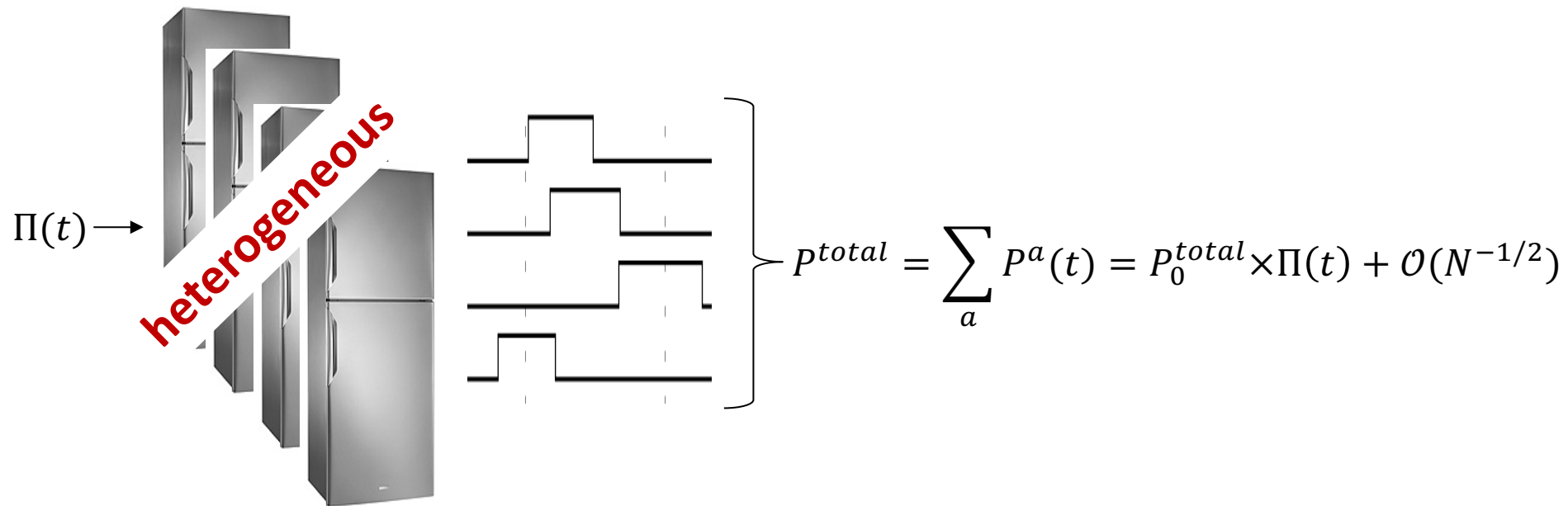
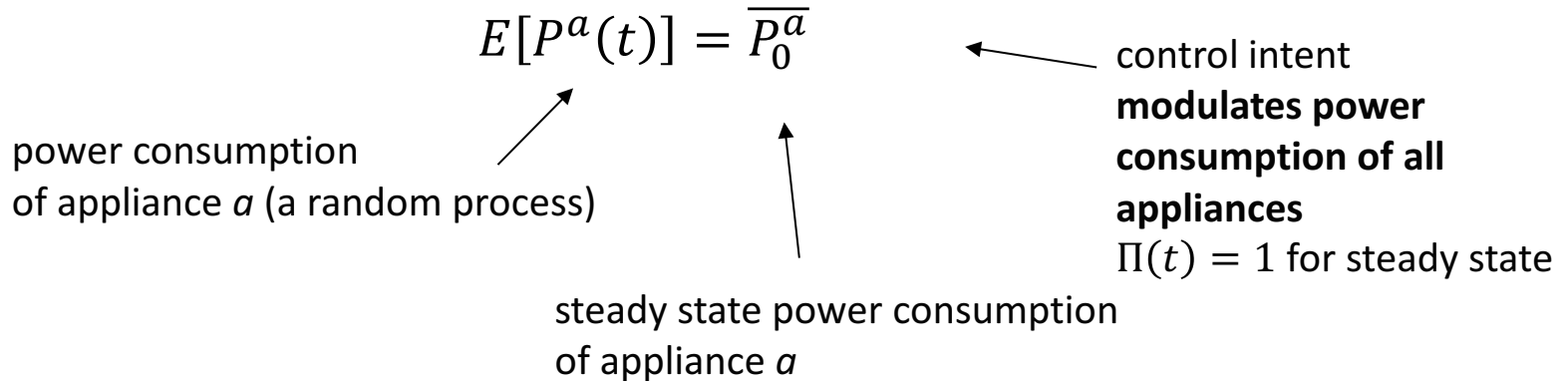
Goals and actions are decided centrally, or in a distributed fashion

Indirect control

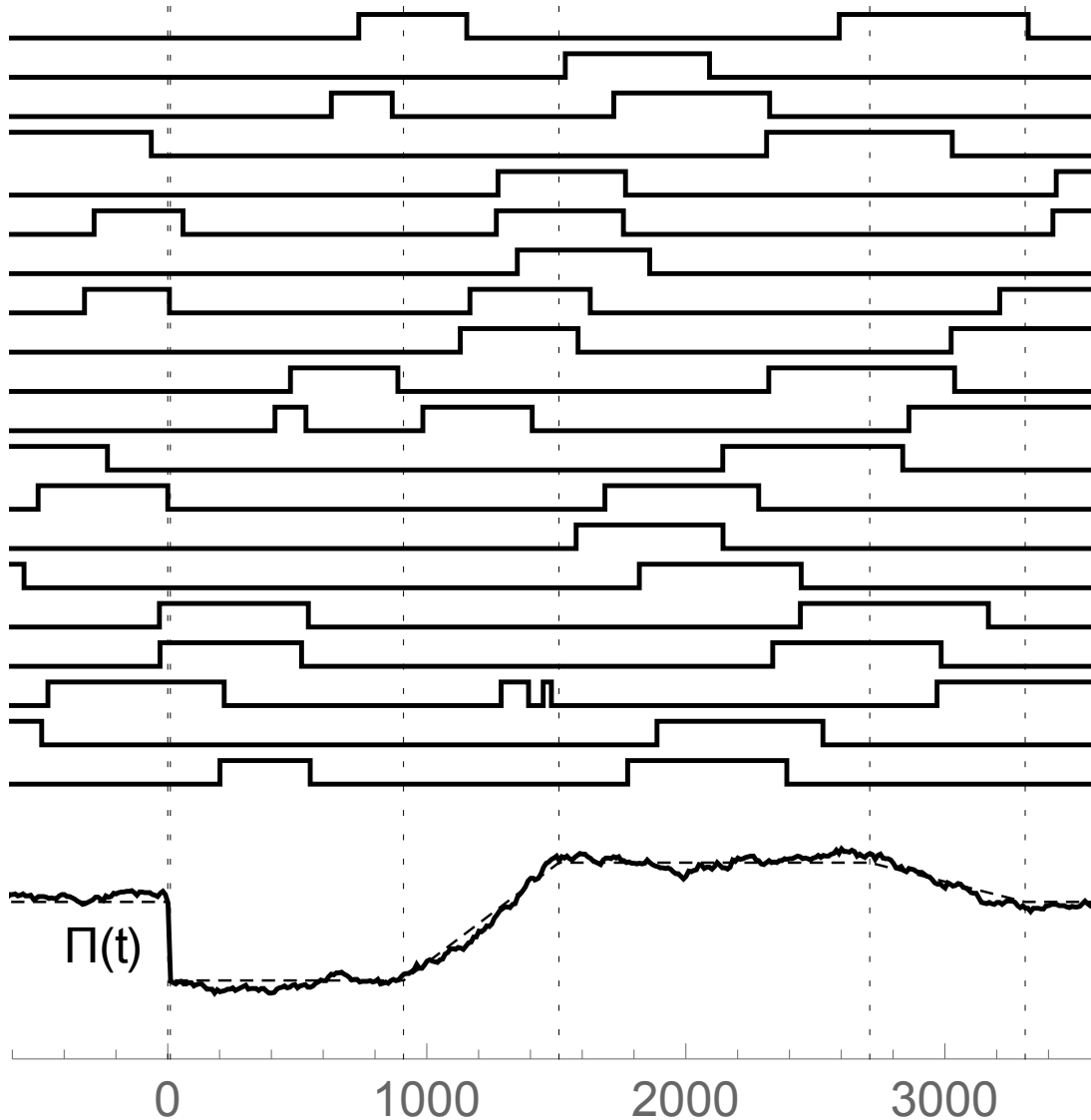
Decentralised actions on the basis of a non-local control signals







Aggregate convergent response



Collectively, **fridges track the reference signal $\Pi(t)$** – even when each appliance is different!

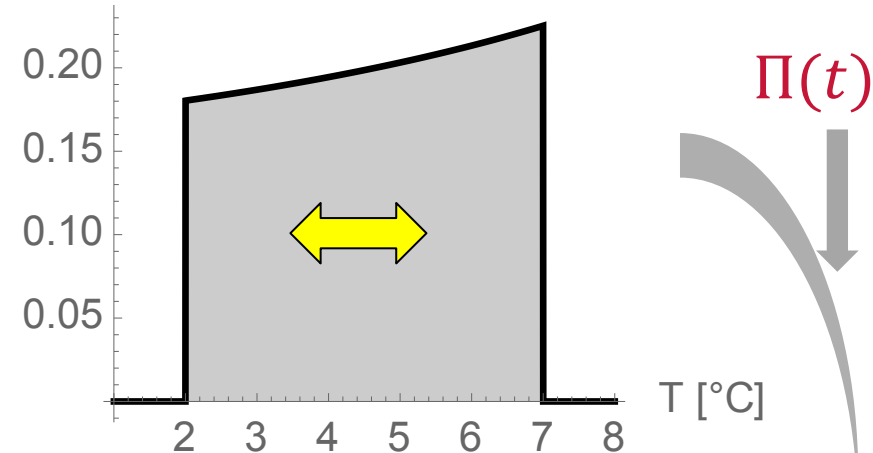
N=1000 domestic refrigerators

- Each appliance knows its **state** and **model**

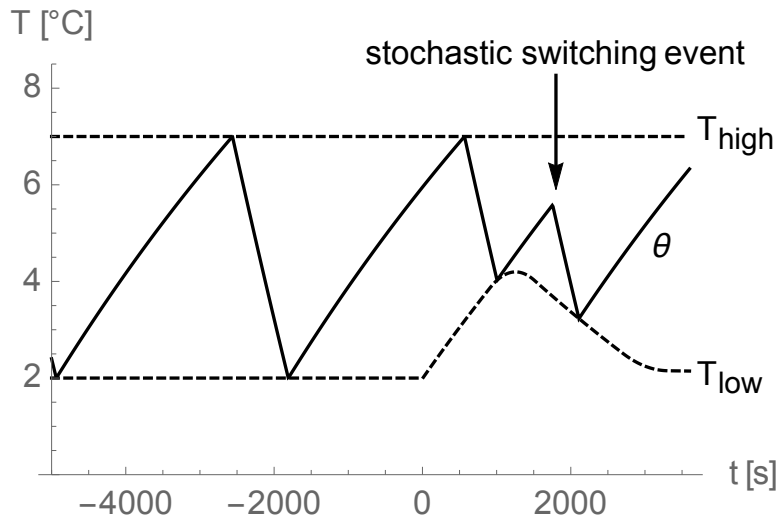
$$\frac{dT(t)}{dt} = \begin{cases} -\alpha(T(t) - T_{on}) & \text{(on)} \\ -\alpha(T(t) - T_{ambient}) & \text{(off)} \end{cases}$$



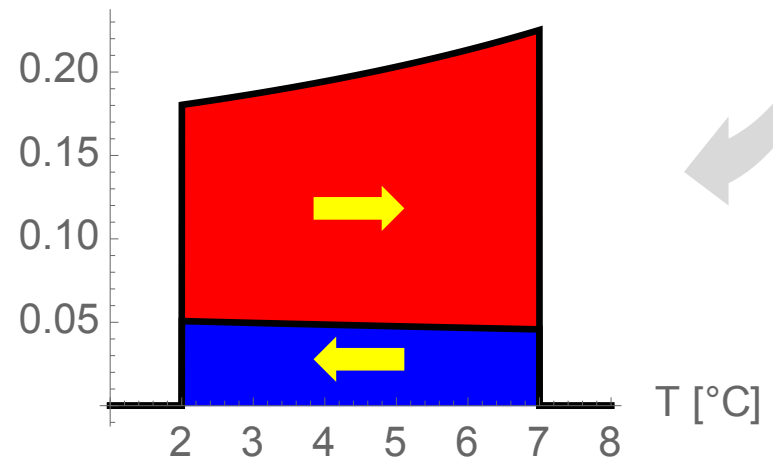
- Construct a **homogeneous 'virtual population'** with random temperatures.



- Determine device-specific actions, based on the actual device temperature



- Manipulate the 'virtual population' to control its (virtual) power consumption in line with $\Pi(t)$.



1. Each appliance knows its **state** and **model**

2. **Construct a *homogeneous* 'virtual population'** with random temperatures.

Each appliance considers itself as a random representative of a population...

4. **Determine device-specific actions,** based on the actual device temperature

3. **Manipulate the 'virtual population'** to control its (virtual) power

...and takes individual actions in line with population objectives

(sub-)population avg temperature

$$\bar{T}(t) = T_{\text{OFF}} - \alpha(T_{\text{OFF}} - \bar{T}_0) \int_{-\infty}^t \Pi(t') e^{-\alpha(t-t')} dt'.$$

$$\beta(t) = \frac{\Pi(t)(T_{\text{OFF}} - \bar{T}_0) - (T_{\text{OFF}} - \bar{T}(t))}{T_{\text{max}} - \bar{T}(t)}.$$

rate of heating/cooling

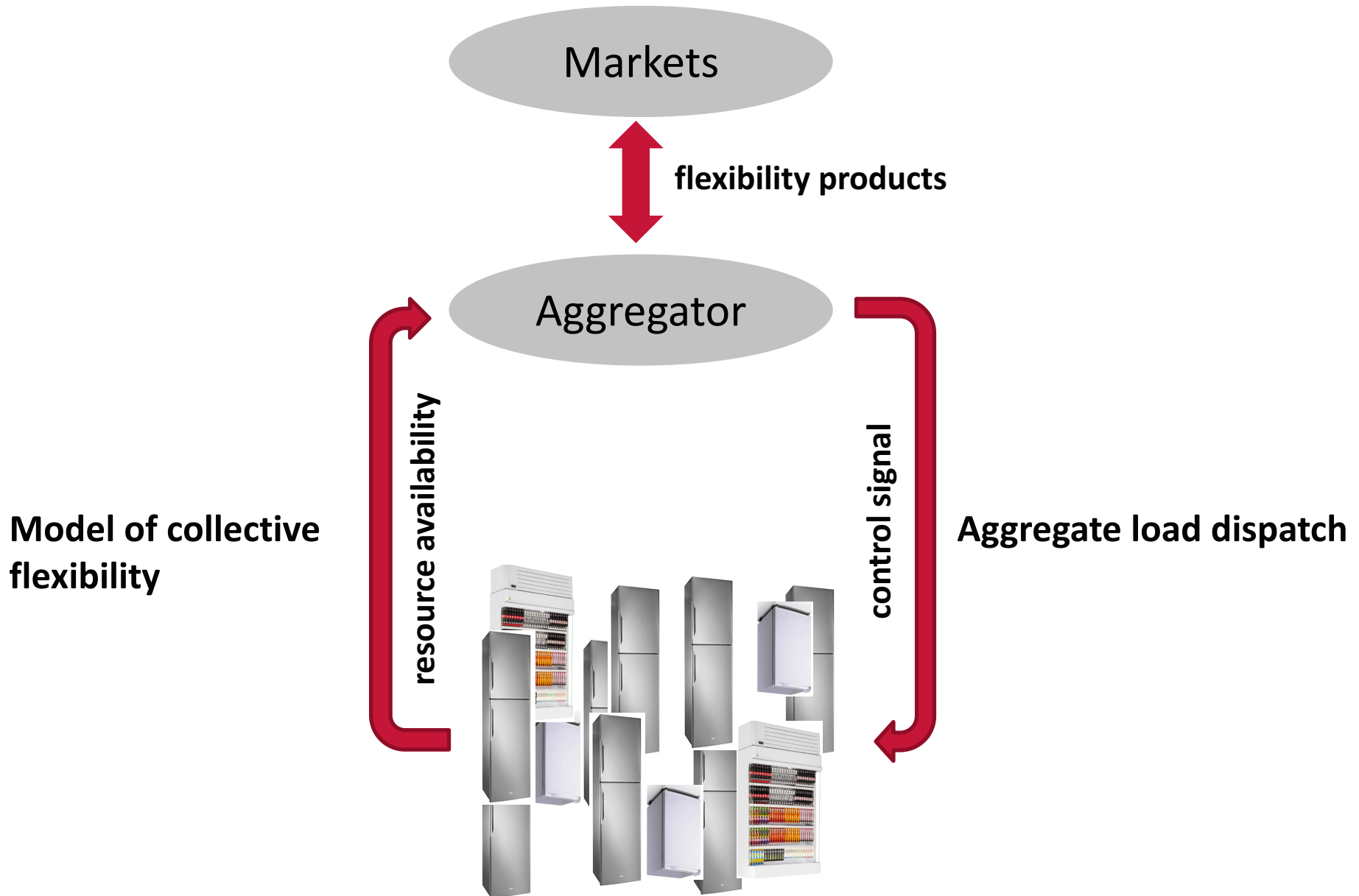
$$v(T, t) = \alpha\beta(t)(T - T_{\text{max}}).$$

switching rates

$$r_{\text{OFF}}^{\text{ON}}(T, t) = \max\left(0, \frac{\Xi(T, t)}{v_{\text{OFF}}(T) - v(T, t)}\right)$$

$$r_{\text{ON}}^{\text{OFF}}(T, t) = \max\left(0, \frac{\Xi(T, t)}{v_{\text{ON}}(T) - v(T, t)}\right).$$

$$\begin{aligned} \Xi(T, t) = & \alpha\tau_{\text{max}} \frac{d\beta(t)}{dt} + \alpha^2 \left(\frac{\hat{\tau}_{\text{OFF}} + \hat{\tau}_{\text{ON}}}{\hat{\tau}_{\text{OFF}}\hat{\tau}_{\text{ON}}} \right) \\ & \times (\tau_{\text{OFF}} + \beta(t)\tau_{\text{max}}) (\tau_{\text{ON}} + \beta(t)\tau_{\text{max}}) \\ & - \alpha^2(1 + \beta(t)) (\tau_{\text{OFF}} + \tau_{\text{ON}} + \beta(t)\tau_{\text{max}}). \end{aligned}$$




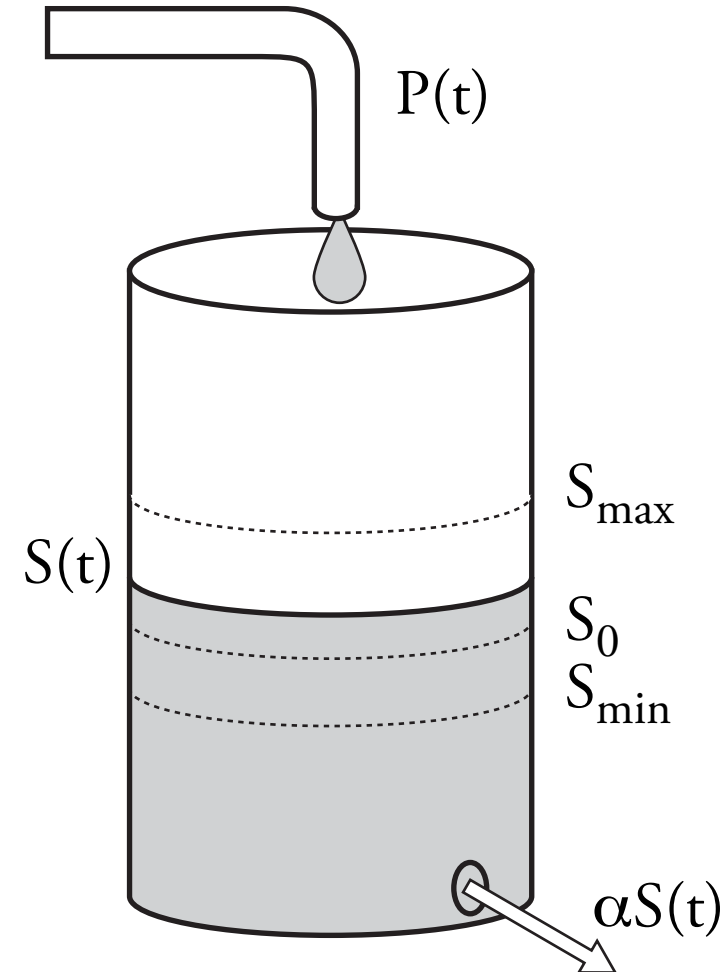
Six-parameter model to describe the flexibility of a homogeneous population

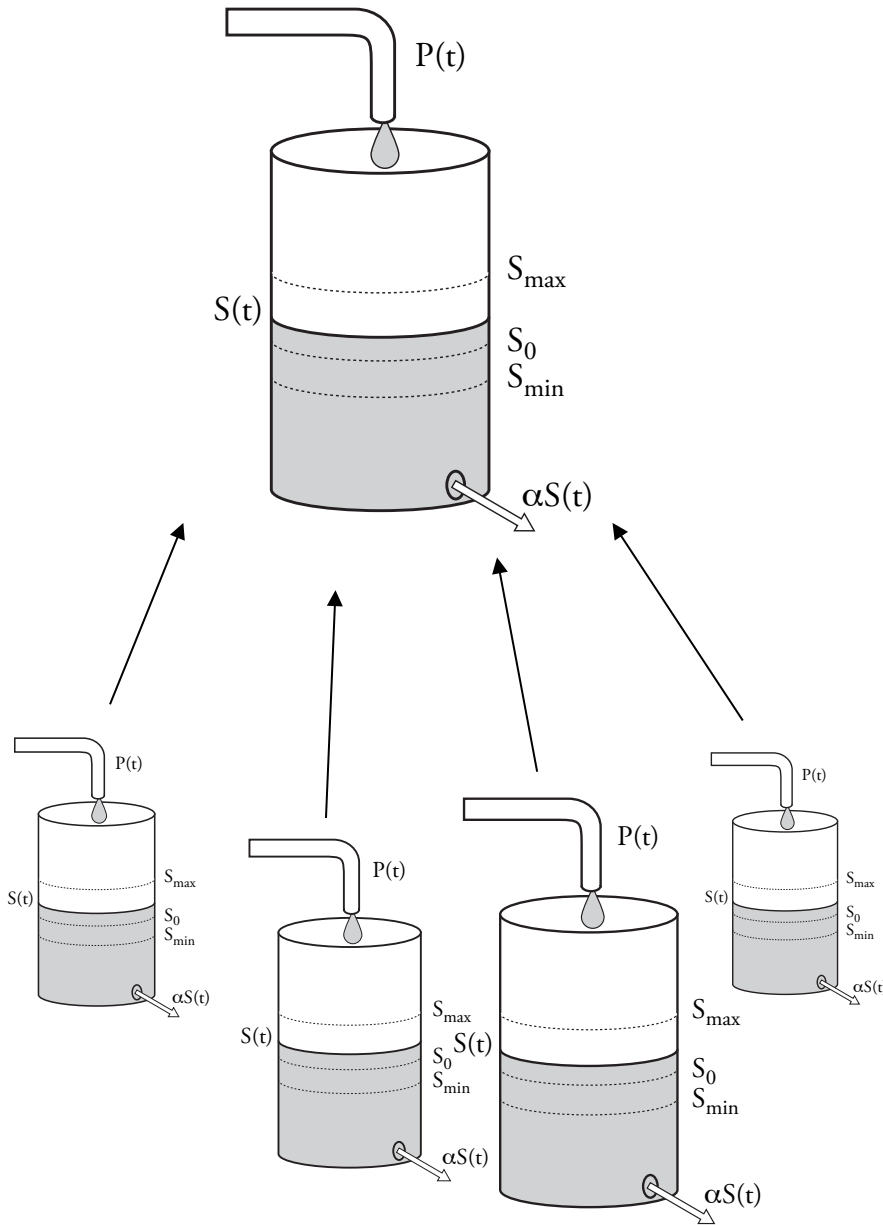
$$\frac{dS(t)}{dt} = P(t) - \alpha S(t)$$

with constraints:

$$\begin{aligned} P_{min} &\leq P(t) \leq P_{max} \\ S_{min} &\leq S(t) \leq S_{max} \\ \int_0^T S(t) dt &= S_0 \end{aligned}$$

preserve the food! 





Heterogeneous models are merged into a conservative **envelope flexibility model**.

The model is **sufficient and linear**, for easy embedding in dispatch models.

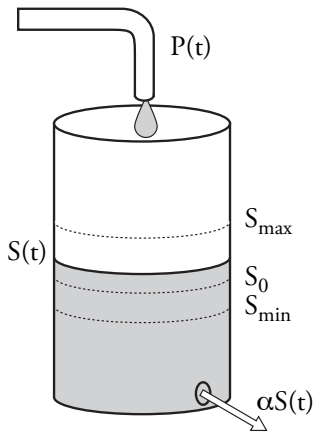
Clustering can be used to match similar appliances.



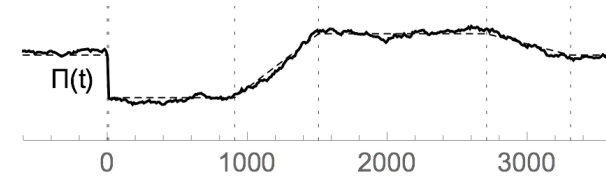
flexibility products



Model of collective flexibility

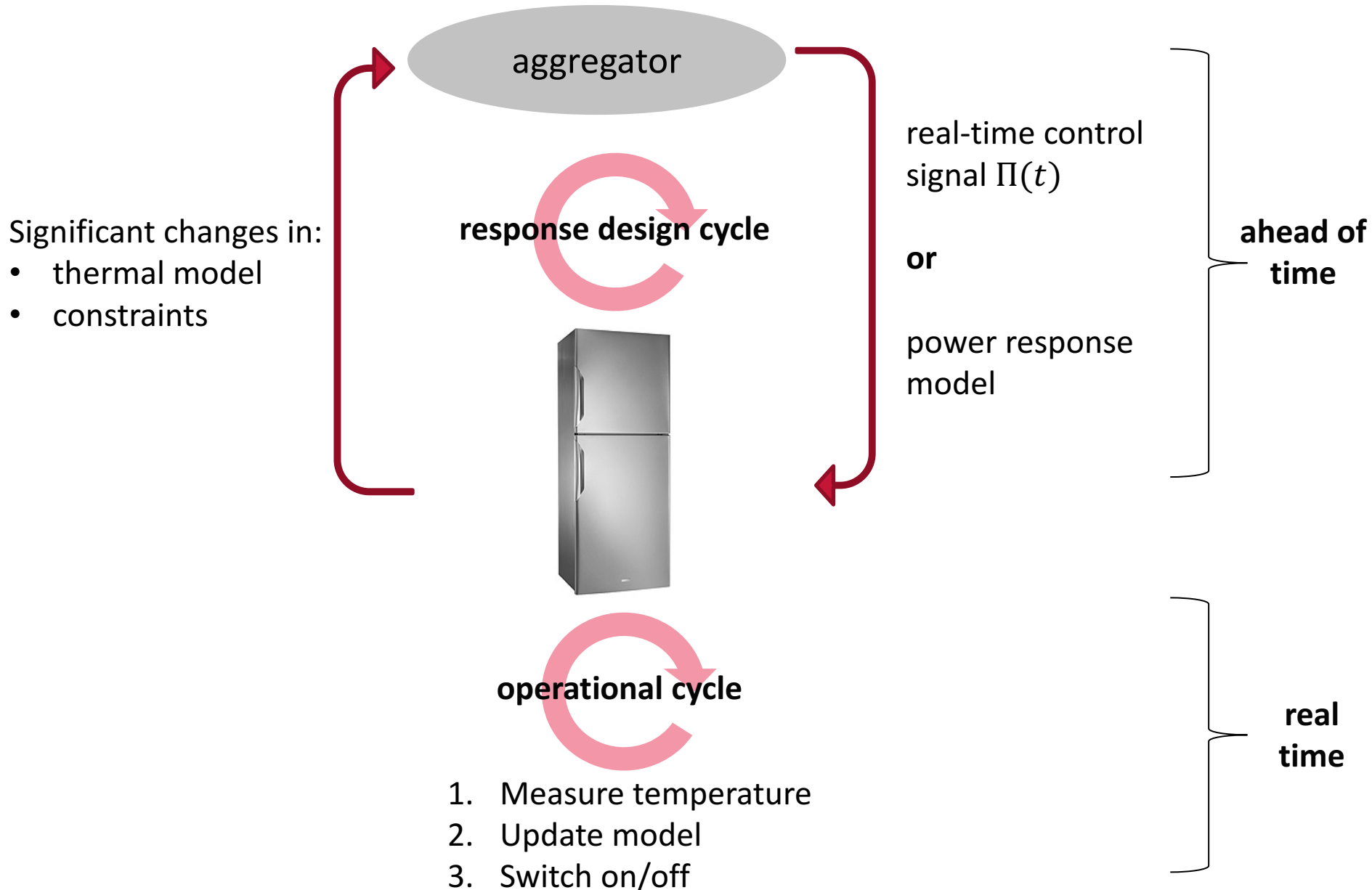


Aggregate load dispatch



Communication requirements

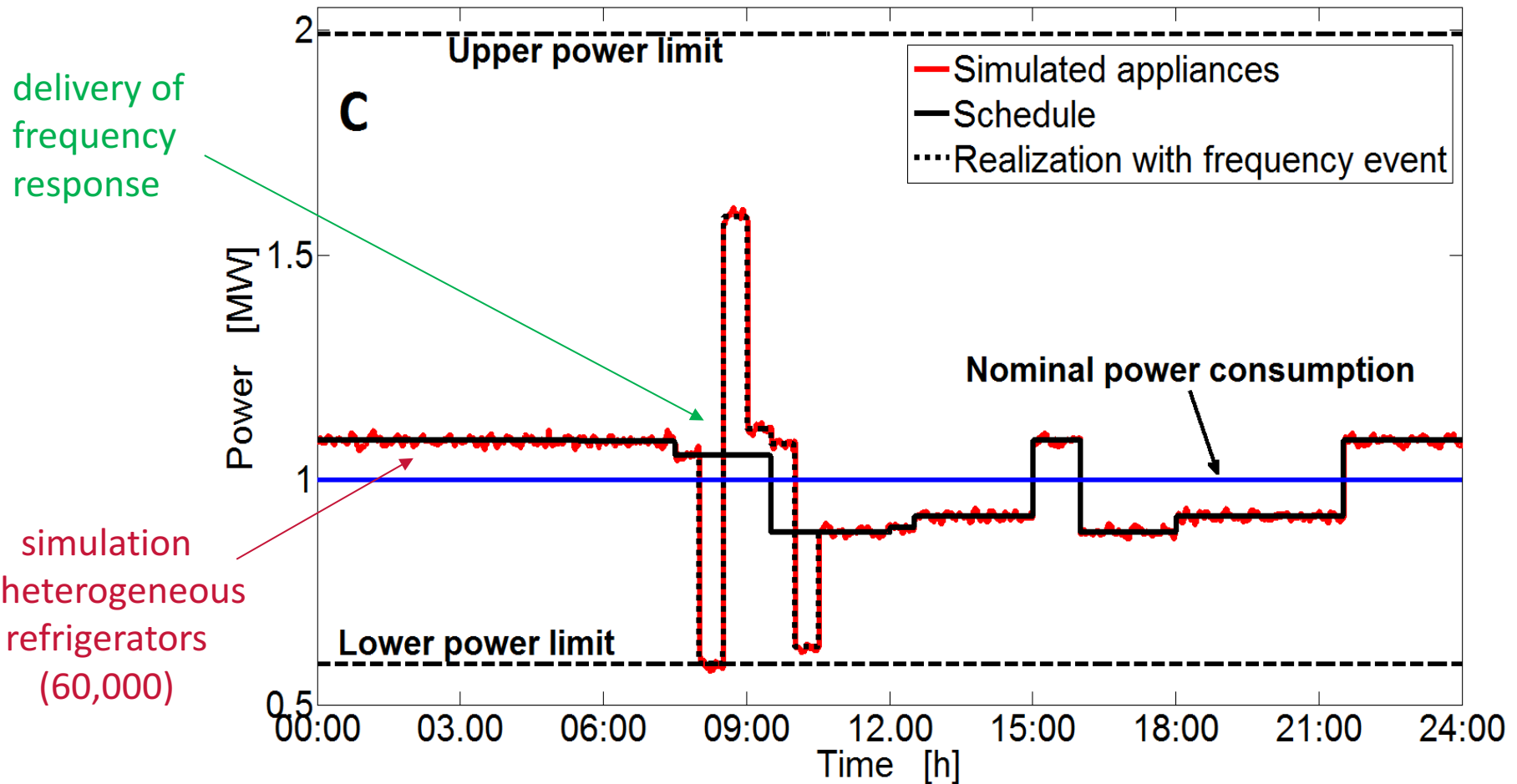
Robust 'semi-autonomous' operation

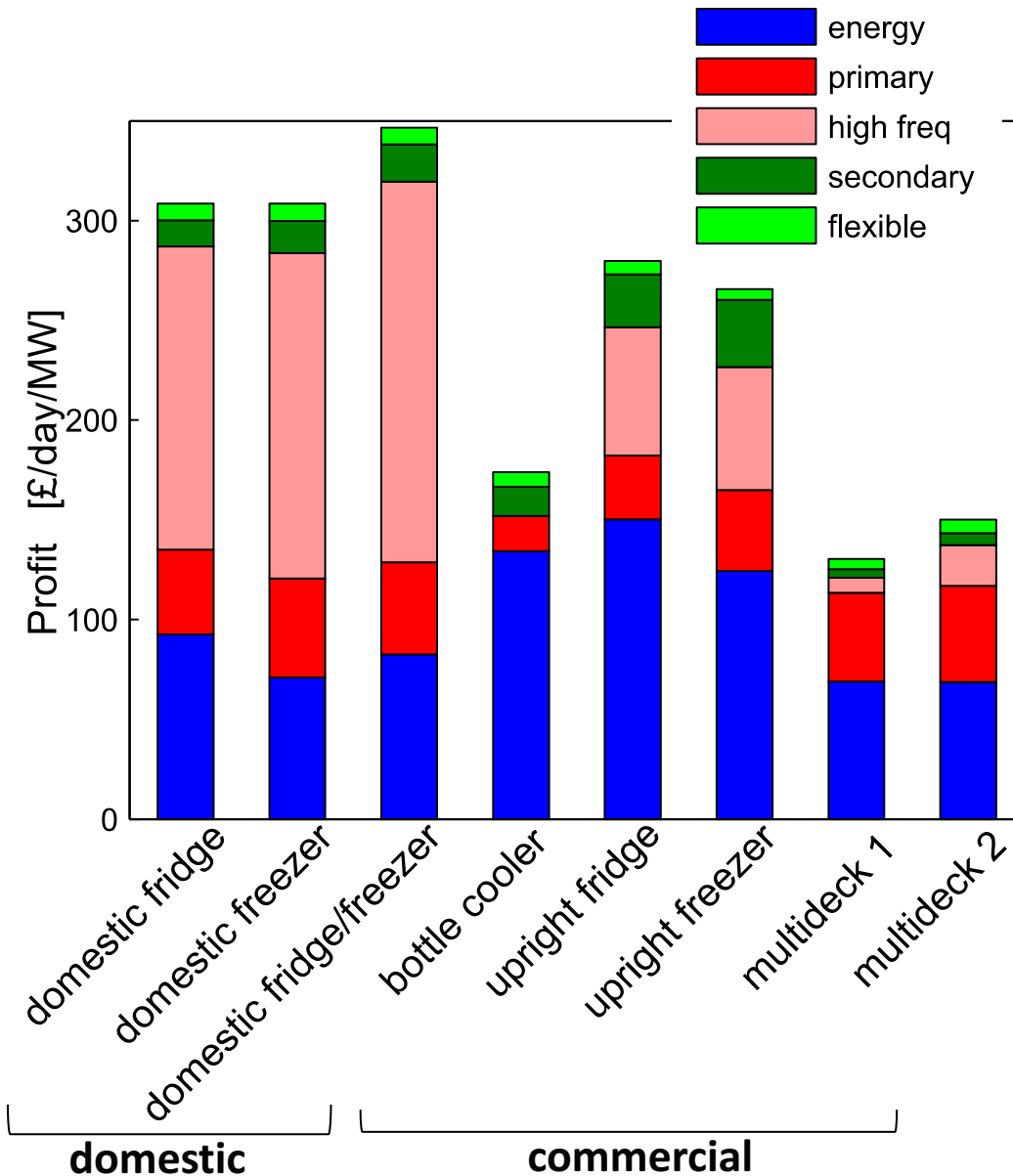


Example: optimal allocation of flexibility

59,524 refrigerators (1MW); 24-hour allocation

Using refrigerators to provide **energy arbitrage** *and* **frequency services**, making optimal use of device flexibility





Service allocations reflect physical characteristics:

- Slow thermal time constants are good for energy arbitrage
- Low duty cycles in domestic appliances leave headroom for high frequency response.

Summary so far

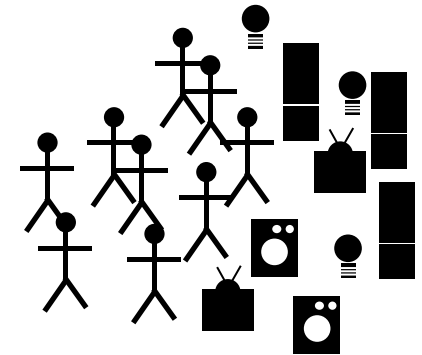
- We have developed a stochastic control scheme that is **nondisruptive, decentralised and accurate**.
- **Semi-autonomous control** separates the communication and operation time scales, and is robust to perturbations and heterogeneity.

New developments

- **Implementation** (Lab tests starting soon)
- **Testing and proving robustness** against ‘things going wrong’ (model misspecification, user actions, etc)
- **Optimal control** of ‘leaky storage’ units

FINAL REMARKS

- The long tail of demand response is substantial, but there are restrictions on control.
- Modelling and quantification of uncertainty is essential.
- Diversity should be used as an asset, not a hindrance.



Understand response to control signals

- Data-driven modelling to quantify and *predict* response
- Design of experiments for automated model testing and improvement in a business as usual environment

Quantify and mitigate risks

Develop purpose-built decentralised controllers

- *Guarantee* local service quality and *quantify* system service quality
- Ensure fairness of outcomes
- Analyse robustness against disturbances

Design subject to risk and fairness constraints

- Peer-to-peer communication (aka 'the energy internet') *will* give rise to unexpected emergent behaviour.



- Do we need to develop 'grid safety certification' for smart energy appliances?
- Lab tests and demonstrators will not be sufficient; we need simulations and basic analysis.

This research was supported by a Marie Curie Intra European Fellowship within the 7th European Community Framework Programme and by National Grid.



nationalgrid

“Low Carbon London” was funded through the Low Carbon Networks Fund programme, administered by the UK Regulator, Ofgem.

ofgem



s.tindemans@imperial.ac.uk

- **Low Carbon London Project: Data from the Dynamic Time-of-Use Electricity Pricing Trial, 2013**
James Schofield, Richard Carmichael, Simon Tindemans, Mark Bilton, Matt Woolf, Goran Strbac.
(2016). UK Data Service. SN: 7857
- **A baseline-free method to identify responsive customers on dynamic time-of-use tariffs**
James Schofield, Simon Tindemans, Goran Strbac
arXiv:1605.08078
- **Resilience performance of smart distribution networks**
Simon Tindemans, Predrag Djapic, James Schofield, Tatiana Ustinova and Goran Strbac
Report D4 for the “Low Carbon London” LCNF project, 2014.
- **Residential consumer responsiveness to time varying pricing**
James Schofield, Richard Carmichael, Simon Tindemans, Matt Woolf, Mark Bilton and Goran Strbac
Report A3 for the “Low Carbon London” LCNF project, 2014.
- **Decentralised control of thermostatic loads for flexible demand response.**
Simon Tindemans, Vincenzo Trovato, Goran Strbac
IEEE Transactions on Control Systems Technology (2015)
- **The Leaky Storage Model for optimal multi-service allocation of thermostatic loads.**
Vincenzo Trovato, Simon Tindemans, Goran Strbac
IET Generation, Transmission & Distribution (2016)
- **Nondisruptive decentralized control of thermal loads with second order thermal models**
Simon Tindemans, Goran Strbac
2016 *IEEE PES General Meeting, Boston.*