

Ecological intuition versus Economic reason.

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Paper with O. Guéant, J.M Lasry.

Climate change, and the discount rate debate.

- Economic « reason » without doubts..
 - Nordhaus (DICE), a growth model with carbon as a factor.
 - Standard discount rates (5%) lead to « lenient policies ».
 - Behind : reference to market rates, explained by
 - Pure rate of time preferences 1-2%
 - Elasticity of marginal utility 1,5, growth rate of 2%.
- An attempt of reconciliation with « ecological intuition » : the Stern review.
 - Puts emphasis on uncertainty and probabilistic assessments.
 - Comprehensive assessments of the costs of damage.
 - Low discount rates :1,1% justified by
 - Pure rate of time preferences of 0,1%.
 - Log utility (Cobb-Douglas).
 - Criticisms.
- Directions for reassessments.
 - Uncertainty (Weitzmann)
 - Stress the specificities of environmental goods.

A two goods model.

- **The model :**
 - **2 goods :**
 - *aggregate consumption good : quantity.*
 - *« environmental quality »*
- **The preferences parameters of generation t : σ', σ**
 - **Utility function :**
 - $v(x_t, y_t) = \{ [x_t^{((\sigma-1)/\sigma)} + y_t^{((\sigma-1)/\sigma)}]^{(\sigma/(\sigma-1))} \}$
 - $V(x_t, y_t) = [1/(1-\sigma')] [v(x_t, y_t)]^{(1-\sigma')}$
 - Comment.
 - **y/x decreases of 1/100, the willingness to pay increases of (1/σ) per 100**
 - Iso-elastic cardinal utility for generation t, constant relative risk aversion σ'

The four parameters world.

- **Elasticity of marginal utility or relative risk aversion $\underline{\sigma'}, \underline{\sigma}$**
 - $\sigma > 1, (< 1)$ moderate, (radical environmentalist.
 - $\underline{\sigma'}$ plays a role in the intensity of redistribution towards the poor..
 - 1,5, 3 ?
- **Intergenerational (social) welfare : $\underline{\delta}$**
 - $U = [1/(1 - \sigma')] \sum_{t=0}^{\text{infini}} \{ (\exp(-\delta t)) [v(x_t, y_t)]^{(1 - \sigma')} \}$
 - **Pure rate of time preferences.. utilitarian.** $\delta \rightarrow 0$, « ethical » viewpoint.
 - Positive (Koopmans).
 - $>$ rate of survival of the planet
- **Economic possibilities : \underline{r} .**
 - **A simplistic view of the growth possibilities : AK model.**
 - **or first take growth rates as given ..**

The concern for environment.

- The concern for environment σ
 - The world is radically different depending on whether σ is greater or smaller than one.
 - Opposes the « radical » environmentalist $\sigma < 1$ and the « moderate » environmentalist $\sigma > 1$.
 - Later, uncertainty bears on σ .
- A world with two goods...
 - Standard discount rate : relative price of the private good period t , vis-à-vis period 0
 - $(\exp(-\sum^T r^*(t)))$
 - Ecological discount rate : relative price of the environmental good $\exp(-\sum^T \beta^*(t))$.
 - « Canonical » Ecological Cost benefit Analysis
 - Generation 0 evaluates an invest (at 0), generating an improv of the environl quality for generation t , value measured with the marginal willingness to pay of generation 0 : multiplied by the « ecological discount rate

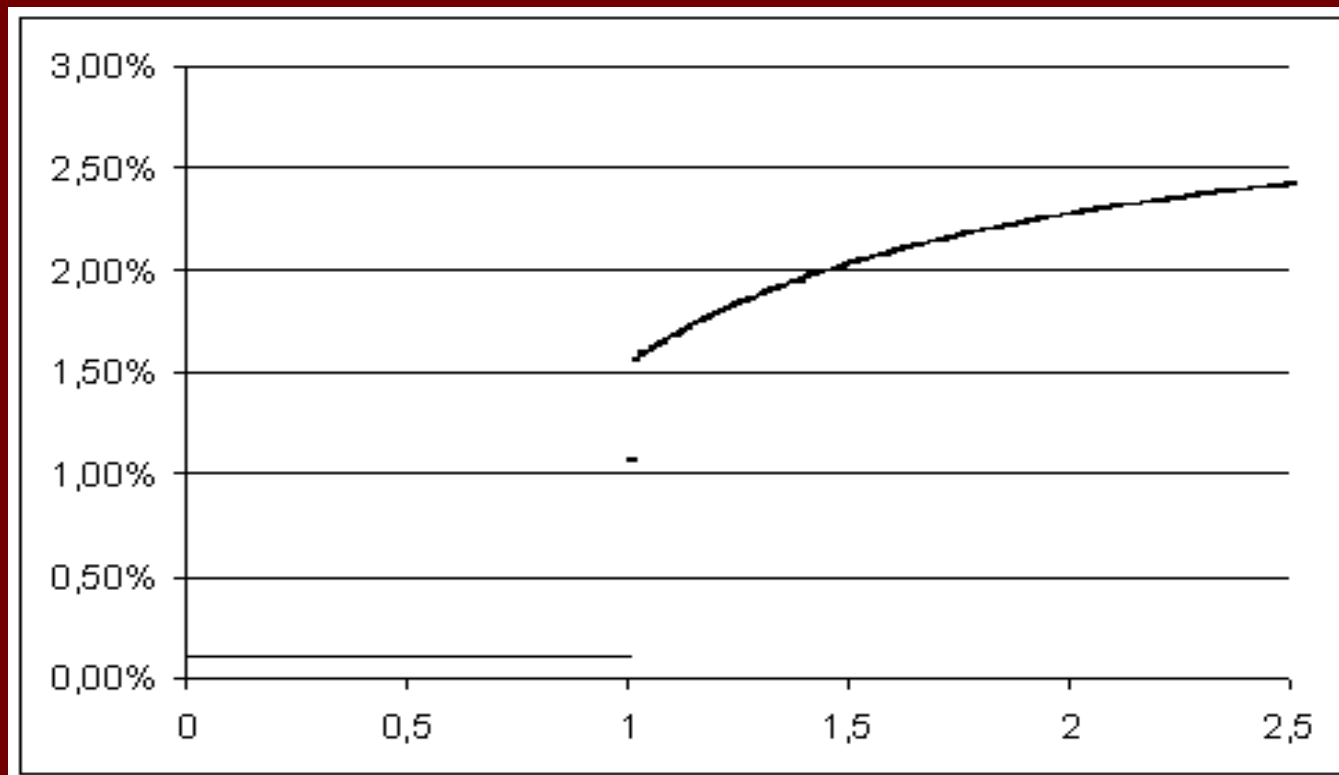
Ecological discount rate from the reform viewpoint.

- ***The reform viewpoint :***
 - *Fixed environmental quality*
 - *Given trajectory of growth rates g*
 - *The long run .*
- ***A basic insight : the relative price effect.***
 - $B = r - (g/\sigma)$
- ***Proposition A : the « moderate » environmentalist.***
 - Standard discount rate : $\text{Min}(g\sigma') + \delta$
 - Ecological long run discount rate : $\lim \rho(T) = \underline{g} [\underline{\sigma}' - (1/\underline{\sigma})] + \delta$
 - $\text{Min}\{g\}[\text{Min}\{\underline{\sigma}'\} - 1/\{\text{Min}\underline{\sigma}\}] : (1)(1,4 - 0,9) = 0,5 \text{ pour cent !}$
- ***Proposition B : the « radical » environmentalist.***
 - Standard discount rate : $(g/\sigma) + \delta$
 - ecological long run discount rate : $\lim \rho(T) = \delta$

The optimum in the 4-parameters world.

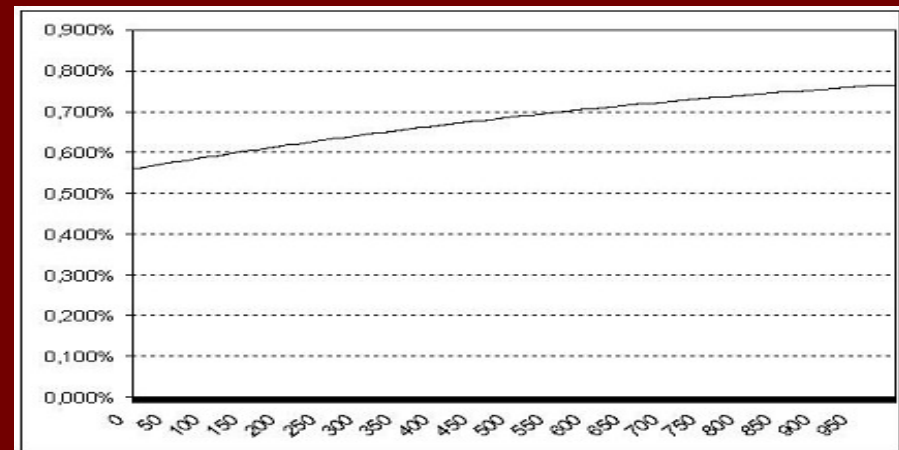
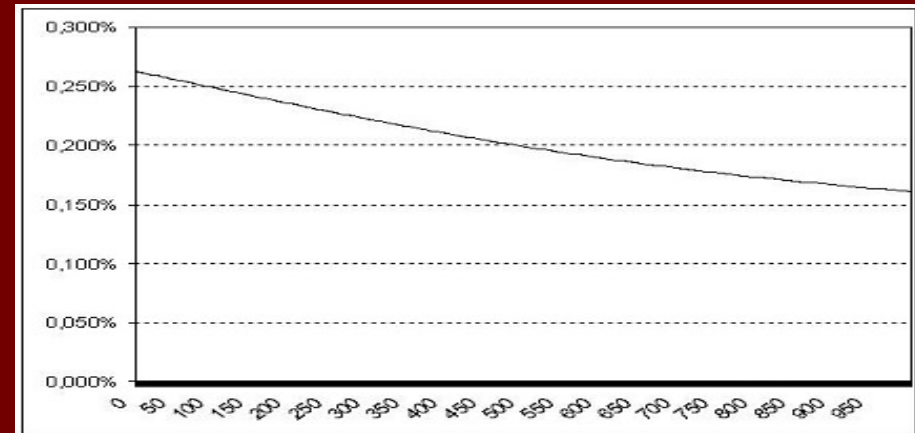
- Constraints.
 - Fixed environmental quality.
 - Fixed interest rate (standard discount rate).
- Results : optimal asymptotic growth with moderate environmental concerns.
 - Asymptotic growth rate : $g^* = (r - \delta) / \sigma'$
 - Ecological discount rate : $B^* = [1 - 1/(\sigma'\sigma)]r + 1/(\sigma'\sigma) \delta$.
- Optimal growth with radical environmental concerns :
 - Asymptotic growth rate : $g^* = \sigma(r - \delta)$
 - Ecological discount rate : $B^* = \delta$.
- Discontinuity and continuity :
 - At each t , the optimal trajectory, as well as the ecological discount rate, is a continuous function of σ

Long run ecological discount rate as a function of sigma.

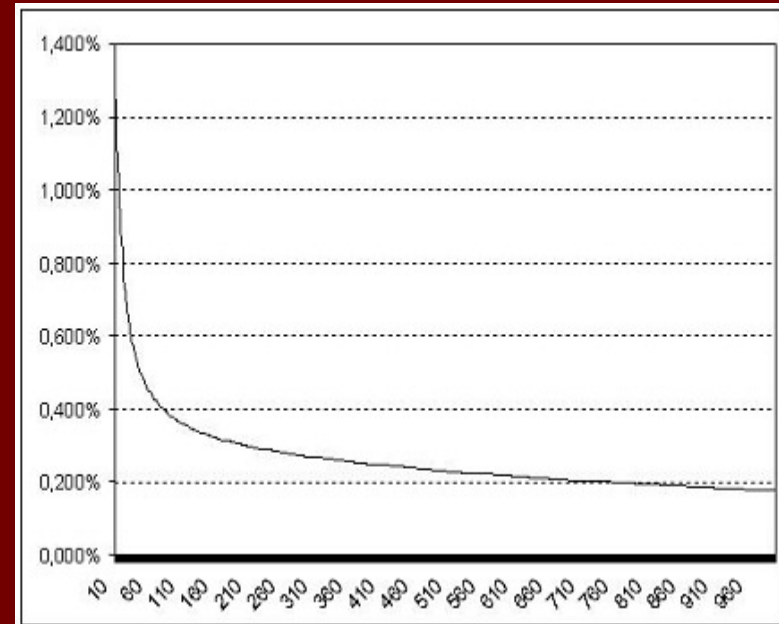
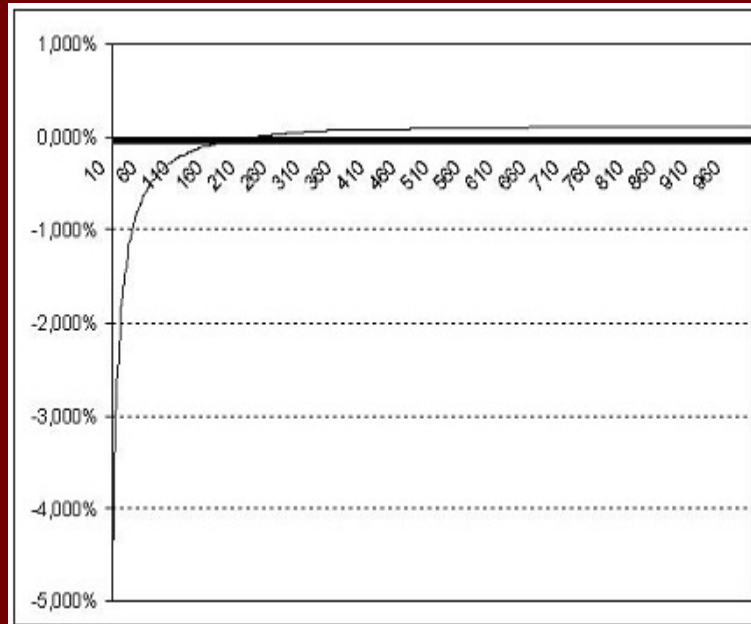


The dynamics of « ecological discount rates ».

- The dynamic of optimal growth rates ($\sigma'\sigma > 1$)
 - $\sigma < 1$, $g^*(t)$ is increasing.
 - $\sigma > 1$, $g^*(t)$ is decreasing.
- The dynamics of ecological discount rates
 - $\sigma < 1$,
 - $B^*(t)$ is decreasing
 - and converges to δ .
 - $\sigma > 1$,
 - $B^*(t)$ is increasing
 - and conv to : $r - (r - \delta) / \sigma'\sigma$
- $\sigma' = 1,5$,
 - $\sigma =$
 - 0,8,
 - 1,2,
- $\delta = 0,1$, $r = 2\%$



Ecological return : the wealth effect.



Valuing an irreversible damage to the environment.

- The question :
 - Consider an irreversible damage to the environment
 - Generation 0 is willing to pay x to avoid the damage for itself.
 - How much should it be willing to pay, considering other generations ?
 - The answer is mx , $m > 1$.
- An Answer : A Bound on m , with a broad validity range ?
 - Consider $a = [1 - 1/(\sigma'\sigma)]r + 1/(\sigma'\sigma)\delta$
 - $m > 1/a$, irrespective of σ .
- Examples :
 - $\sigma' = 1,5$, $\delta = 0,1\%$, $r = 2\%$, $\sigma = 0,8$,
 - $m > 300$
 - $\sigma' = 1,5$, $\delta = 1\%$, $r = 3\%$
 - $\sigma = 1,2$, bound 52,94, actual m : 61, 49.
 - $\sigma = 0,8$, bound 75, actual m : 86, 68.
 - $\sigma' = 1,5$, $\delta = 0,1\%$, $r = 3\%$,
 - $\sigma = 0,8$, $m = 200$,
 - $\sigma = 1,2$, $m = 75$.

Introducing uncertainty on σ

- Modelling :
 - The elasticity of substitution σ is **uncertain**.
 - **the uncertainty on σ** remains steady until period τ
 - It will be fully revealed at time τ .
- Question 1 : what about the long run « ecological discount rate » ?
 - The long run ecological discount rate is δ . (WPP)
- Question 2 :
 - Revelation of the uncertainty comes together with an « ecological » accident,
 - the present generation would be willing to pay x for avoiding this accident to itself under the assumption that the moderate environmentalist hypothesis has probability $(1-p)$
 - How much should it be prepared to pay to avoid the « accident » that will concern all generations following τ

Strong precautionary principle.

- Question 2 :
 - Revelation of the uncertainty comes together with an « ecological » accident,
 - the present generation would be willing to pay
 - How much should it be prepared to pay to avoid the « accident » that will concern all generations following τ
- WPP : ecological discount rate tends to delta
- Answer 2 : SPP
 - $a = [1 - 1/(\sigma' \sigma)]r + 1/(\sigma' \sigma) \delta$
 - $m > \exp(-a(h)\tau) f(p, \tau)$
 - $f > ((1-p)/a(h) + p/a(l))$ and concave.
 - $\lim(\tau) [f(p, \tau) = a(l)]$
- Back of the envelope computation.

m as a function of the probability of accident

